



SAGA Working Paper  
March 2004

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Strategies and Analysis for Growth and Access (SAGA) is a project of Cornell and Clark Atlanta Universities, funded by cooperative agreement #HFM-A-00-01-00132-00 with the United States Agency for International Development.



# Robust Multidimensional Spatial Poverty Comparisons in Ghana, Madagascar, and Uganda<sup>1</sup>

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## Abstract

We investigate spatial poverty comparisons in three African countries using multidimensional indicators of well-being. The work is analogous to the univariate stochastic dominance literature in that we seek poverty orderings that are robust to the choice of multidimensional poverty lines and indices. In addition, we wish to ensure that our comparisons are robust to aggregation procedures for multiple welfare variables. In contrast to earlier work, our methodology applies equally well to what can be defined as "union", "intersection," or "intermediate" approaches to dealing with multidimensional indicators of well-being. Further, unlike much of the stochastic dominance literature, we compute the sampling distributions of our poverty estimators in order to perform statistical tests of the difference in poverty measures.

We apply our methods to two measures of well-being, the log of household expenditures per capita and children's height-for-age z-scores, using data from the 1988 Ghana Living Standards Survey, the 1993 *Enquête Permanente auprès des Ménages* in Madagascar, and the 1999 National Household Survey in Uganda. Bivariate poverty comparisons are at odds with univariate comparisons in several interesting ways. Most importantly, we cannot always conclude that poverty is lower in urban areas from one region compared to rural areas in another, even though univariate comparisons based on household expenditures per capita almost always lead to that conclusion.

**Keywords:** Multidimensional Poverty, Stochastic Dominance, Ghana, Madagascar, Uganda

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<sup>1</sup> This research is supported by the SAGA project, funded by USAID cooperative agreement #HFM-A-00-01-00132-00 with Cornell and Clark-Atlanta Universities, and by the Poverty and Economic Policy (PEP) network of the IDRC. For more information, see <http://www.saga.cornell.edu> and [www.pep-net.org](http://www.pep-net.org).

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# 1. Introduction

It is common to assert that poverty is a multi-dimensional phenomenon, yet most empirical work on poverty, including spatial poverty, uses a one-dimensional yardstick to judge a person's well-being, usually household expenditures or income *per capita* or per adult equivalent. When studies use more than one indicator of well-being, poverty comparisons are either made for each indicator independently of the others,<sup>3</sup> or are performed using an arbitrarily-defined aggregation of the multiple indicators into a single index.<sup>4</sup> In either case, aggregation across multiple welfare indicators, and across the welfare statuses of individuals or households, requires specific aggregation rules, and no such rules can be devised such as to receive unanimous approval.<sup>5</sup> Multidimensional poverty comparisons also require estimation of multidimensional poverty lines, a procedure that is ethically and empirically problematic even in a unidimensional setting.

Taking as a starting point our conviction that multidimensional poverty comparisons are ethically and theoretically attractive, our purpose in this paper is to apply quite general methods for multidimensional poverty comparisons to the particular question of spatial poverty in three African countries, Ghana, Madagascar, and Uganda. We have developed the relevant welfare theory and accompanying statistics elsewhere (Duclos, Sahn, and Younger, 2003). Our purpose in this paper is to give an intuitive explanation of the methods, and to show that they are both tractable and useful when applied to the question of spatial poverty in Africa.

We start in section 2 by considering poverty comparisons that involve two or more measures of well-being, and by asking whether poverty is lower in population A than in population B. Here, we make an important distinction between intersection and union definitions of poverty.<sup>6</sup> If we measure well-being in the dimensions of income and height, say, then a person could be considered poor if her income falls below an income poverty line *or* if her height falls below a height poverty line. We may define this as a union definition of multidimensional poverty. An intersection definition, however, would consider a person to be poor only if she falls below *both* poverty lines. In contrast to earlier work, the tests that we use are valid for both definitions. In fact, they are valid for any choice of intermediate definitions for which the poverty line in one dimension is a function of well-being measured in the other dimension.

Throughout, our poverty comparisons use the dominance approach initially developed in Atkinson (1987) and Foster and Shorrocks (1988a,b,c) in a unidimensional context.<sup>7</sup> It is well-known that one important advantage of this approach is that it is capable of generating poverty orderings that are robust to the choice of a poverty index over broad classes of indices – the orderings are "poverty-measure robust." In our multidimensional context, this further means robustness over the

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<sup>3</sup> This would involve, say, comparing incomes across regions, and then mortality rates across regions, and so on.

<sup>4</sup> The best-known example of this is the Human Development Index of the UNDP (1990), which uses a weighted mean of some averaged indicators across the population.

<sup>5</sup> Such rules have been the focus of some of the recent literature: see for instance Tsui (2002) and Bourguignon and Chakravarty (2003). Bourguignon and Chakravarty (2002) also give several interesting examples in which poverty orderings vary with the choice of aggregation rules.

<sup>6</sup> For further recent discussion of this, see Bourguignon and Chakravarty (2003,2002), Atkinson (2002) and Tsui(2002).

<sup>7</sup> Atkinson and Bourguignon (1982,1987) first used this approach in the context of multidimensional social welfare. See also Crawford (1999).

manner in which multidimensional indicators interact to generate overall individual well-being. As mentioned above, our orderings are also "poverty-line robust" in the sense of being valid for the choice of any poverty frontier over broad domains and union, intersection, or intermediate poverty domains. Again, given the well-known sensitivity of many poverty comparisons to the choice of poverty lines, and the difficulty of choosing the "right" poverty line, we feel that this is an important contribution.

Section 3 applies these methods to spatial poverty comparisons in Ghana, Madagascar, and Uganda. In particular, we compare poverty across region and area (urban/rural) in the dimensions of household expenditures per capita and nutritional status for children under the age of five. Univariate comparisons based on expenditures alone almost always show greater poverty in rural areas in any one region than in urban areas in any other. Bivariate comparisons, however, are less likely to draw this conclusion, for a variety of reasons that we discuss.

Previous work on multidimensional poverty comparisons has ignored sampling variability, yet this is fundamental if the study of multidimensional poverty comparisons is to have any practical application. This paper's poverty comparisons are all statistical, using consistent, distribution-free estimators of the sampling distributions of the statistics of each poverty comparison.

## **2. Methods to compare poverty with multiple indicators of well-being**

### **2.1. Data**

The data for this study come from the 1988 Ghana Living Standards Survey, the 1993 *Enquête Permanente auprès des Ménages* in Madagascar, and the 1999 National Household Survey in Uganda. All of these are nationally representative, multi-purpose household surveys. The first measure of well-being that we use is per capita household expenditures, the standard variable for empirical poverty analysis in developing countries. The second is children's height-for-age z-score (HAZ), which measures how a child's height compares to the median of the World Health Organization reference sample of healthy children (WHO 1983). In particular, the z-scores standardize a child's height by age and gender as follows:

$$z\text{-score} = \frac{x_i - x_{median}}{\sigma_x},$$

where  $x_i$  is a child's height,  $x_{median}$  is the median height of children in a healthy and well-nourished reference population of the same age and gender, and  $\sigma_x$  is the standard deviation from the mean of the reference population. Thus, the z-score measures the number of standard deviations that a child's height is above or below the median for a reference population of healthy children of her/his age and gender.

The nutrition literature includes a wealth of studies showing that in poor countries children's height is a particularly good summary measure of children's general health status (Cole and Parkin 1977; Mosley and Chen 1984; WHO 1995). As summarized by Beaton et al (1990), growth failure is

“...the best general proxy for constraints to human welfare of the poorest, including dietary inadequacy, infectious diseases and other environmental health risks.” They go on to point out that the usefulness of stature is that it captures the “...multiple dimensions of individual health and development and their socio-economic and environmental determinants (p. 2).” In addition, HAZ is an interesting variable to consider with expenditures per capita because the two are, surprisingly, not highly correlated, so that they capture different dimensions of well-being (Appleton and Song 1999).<sup>8</sup>

## **2.2. Univariate Poverty Dominance Methods**

The theoretical and statistical bases for the methods that we use in this paper are developed in Duclos, Sahn, and Younger (2003). In this section, we give an intuitive presentation only. Even though our goal is to make multidimensional poverty comparisons, it is easier to grasp the intuition with a one-dimensional example. Consider, then, the question addressed in Appleton (2001): did poverty decline in Uganda in the 1990s? By far the most common way to answer this question is to:

- 1) choose a poverty line, often based on the expenditure needed to satisfy basic caloric requirements along the lines of Ravallion and Bidani (1994);
- 2) choose a poverty measure, usually a Foster-Greer-Thorbecke (FGT) measure, too often the headcount; and
- 3) calculate poverty at two or more points in time, and compare.

This approach has two weaknesses: it depends on the particular poverty line chosen, and it depends on the particular poverty measure chosen. Setting the poverty line is an imprecise art, and it is possible that choosing a different, equally defensible, poverty line will reverse one’s conclusions. That is, using one poverty line, poverty is found to decline over time, while at another, it is found to increase. In addition, it is possible that one particular poverty measure will show poverty declining while another will show it increasing.

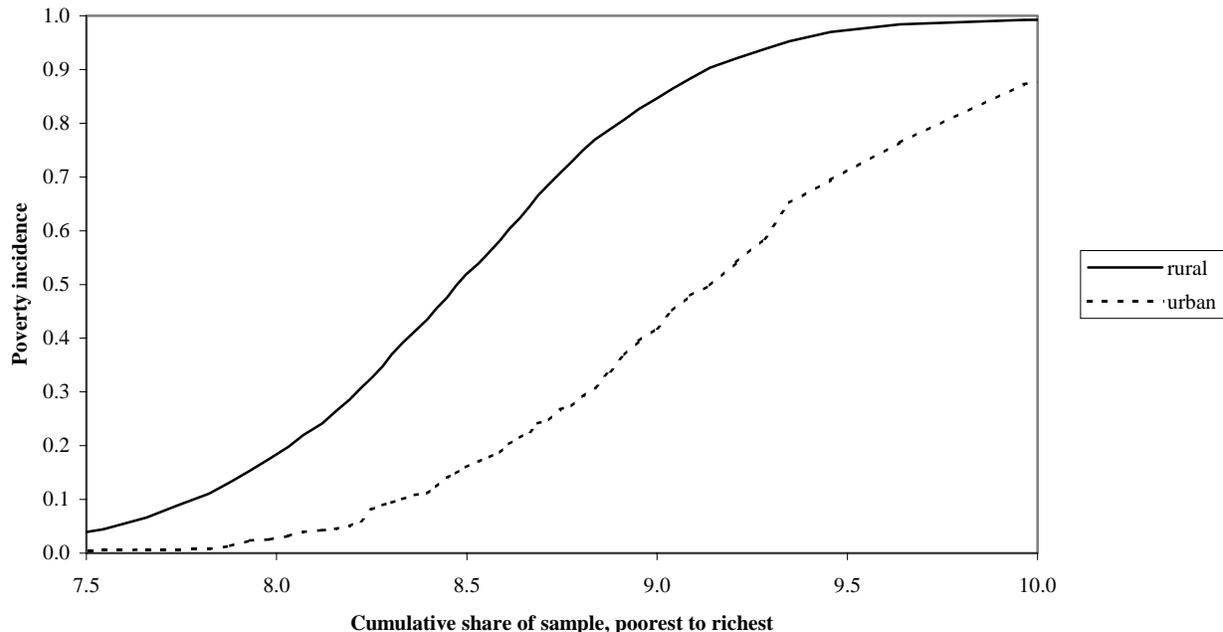
The dominance approach to poverty analysis aims to avoid these problems by making poverty comparisons that are robust to the poverty line selected and the poverty measure selected. Consider Figure 1, which displays the cumulative density functions (cdf) – or distribution functions<sup>9</sup> – for real household expenditures per capita in urban and rural areas of Uganda in 1999. The graph makes clear that no matter which poverty line one chooses, the headcount poverty index (the share of the sample that is poor) will always be lower for urban areas than for rural. Thus, this sort of poverty comparison is robust to the choice of a poverty line.

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<sup>8</sup> Pradhan, Sahn, and Younger (2003) give a more thorough defense of using children’s height as a welfare measure.

<sup>9</sup> The cumulative density function graphs the share of observations in a sample that fall below a given per capita expenditure level against that expenditure level itself. If we think of the values on the x-axis as potential poverty lines – the amount that a household has to spend per capita in order not to be poor – then the corresponding value on the y-axis would be the headcount poverty rate – the share of people whose expenditure is below that particular poverty line. Note that this particular cumulative density function is sometimes called a “poverty incidence curve.”

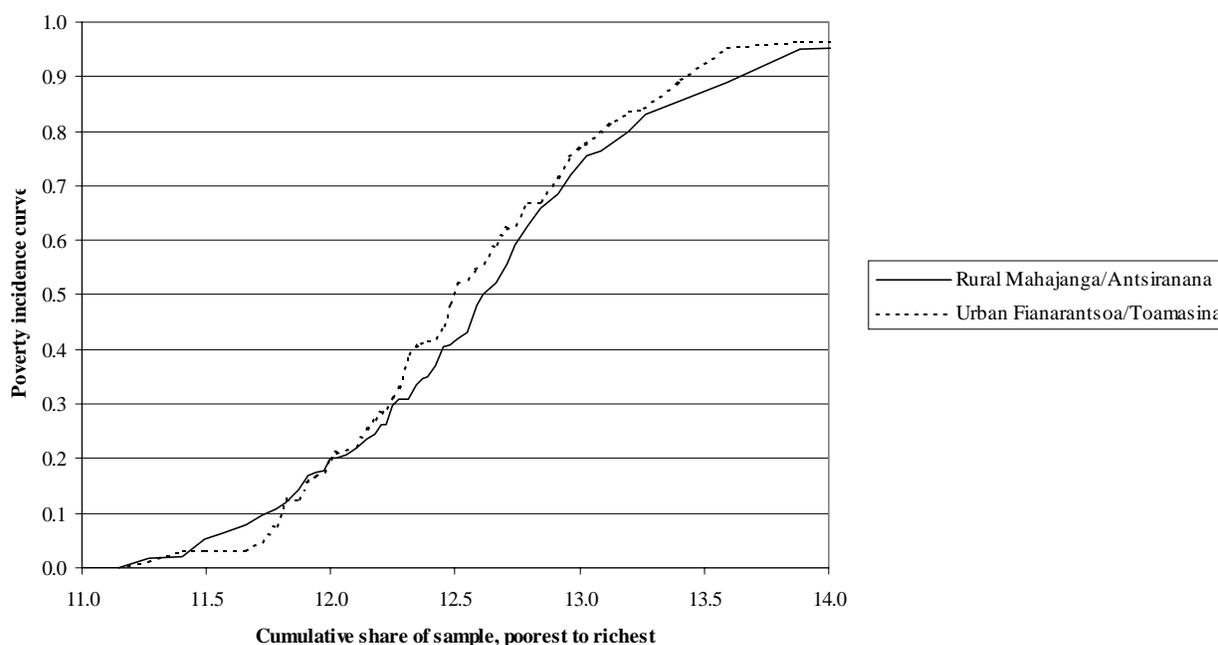
Figure 1 - Poverty Incidence Curves, Urban and Rural Areas of Uganda, 1999



What is less obvious is that this type of comparison also allows us to draw conclusions about poverty according to a very broad class of poverty measures. In particular, the work of Atkinson (1987) and Foster and Shorrocks (1988a,b,c) establishes that if the poverty incidence curve for one sample is everywhere below the poverty incidence curve for another over a bottom range of poverty lines, then poverty will be lower in the first sample for all those poverty lines and for all poverty measures that obey two conditions, that of being non-decreasing and anonymous. By non-decreasing, we mean that if any one person’s income increases, then the poverty measure cannot increase as well. By anonymous, we mean that it does not matter which person occupies which position or rank in the income distribution. It is helpful to denote as  $\Pi^1$  the class of all poverty measures that have these characteristics.  $\Pi^1$  includes virtually every standard poverty measure. It should be clear that the latter two characteristics of the class  $\Pi^1$  are entirely unobjectionable.

Comparing cumulative density curves as in Figure 1 thus allows us to make a very general statement about poverty in urban and rural Uganda: for any reasonable poverty line and for the class of poverty measures  $\Pi^1$ , poverty is lower in urban than rural areas. This is called “first-order poverty dominance.” The generality of such conclusions makes poverty dominance methods attractive. However, such generality comes at a cost. If the cumulative density functions cross one or more times, then we do not have a clear ordering – we cannot say whether poverty is lower in one region or the other. This is the case in Figure 2, which graphs the cdf’s rural Mahajanga/Antsiranana region and urban Fianarantsoa/Toamasina region in Madagascar in 1993. These curves cross at several points, including some that are well below a “reasonable” poverty line. In such cases, we cannot conclude that poverty was unambiguously lower in one region or the other.

**Figure 2 - Poverty Incidence Curves for Rural Mahajanga/Antsiranana and Urban Fianarantsoa/Toamasina, Madagascar, 1993**



There are two ways to deal with this problem, both of which being conceptually considerably more general than the traditional method of fixing the poverty line and focusing on a single poverty measure. First, it is possible to conclude that poverty in one sample is lower than in another for the same large class of poverty measures, but only for poverty lines up to the first point at which the cdf's cross (for a recent treatment of this, see Duclos and Makdissi, 1999). If reasonable people agree that this crossing point is at a level of well-being safely beyond any sensible poverty line, then this conclusion may be sufficient.<sup>10</sup> Second, it is possible to make comparisons over a smaller class of poverty measures. For example, if we add the condition that the poverty measure respect the Pigou-Dalton transfer principle,<sup>11</sup> then it turns out that we can compare the areas under the cdf's shown in Figure 2. If it is the case that the area under one curve is less than the area under another for a bottom range of reasonable poverty lines, then poverty will be lower for the first sample for all poverty measures that are non-decreasing, anonymous, and that obey the Pigou-Dalton transfer principle. This is called "second-order poverty dominance," and we can call the associated class of poverty measures  $\Pi^2$ . While not as general as first order dominance, it is still quite a general conclusion. Note that we can make this comparison by integrating the two curves in Figure 2, yielding "poverty depth curves," and comparing them to see if one is everywhere above the other.

If the poverty depth curves also cross, then we can proceed to a more restricted set of poverty measures, those that are non-decreasing, anonymous, and that obey the Pigou-Dalton transfer

<sup>10</sup> In the case of Figure 2, that is not likely.

<sup>11</sup> The Pigou-Dalton transfer principle says that a marginal transfer from a richer person to a poorer person should decrease (or not increase) the poverty measure. Again, this seems entirely sensible, but note that it does not work for the headcount whenever a richer person located initially just above the poverty line falls below the poverty line due to the transfer to the poorer person.

principle as well as the transfer sensitivity principle.<sup>12</sup> To make dominance comparisons for this class of poverty measures, called  $\Pi^3$ , we compare the area under the poverty depth curves by integrating them again and checking to see if one is entirely below the other. If so, then we have “third-order poverty dominance.” It is possible to continue integrating the curves in this manner until one dominates the other, but the intuition for the associated classes of poverty measures decreases with the order of the comparisons.

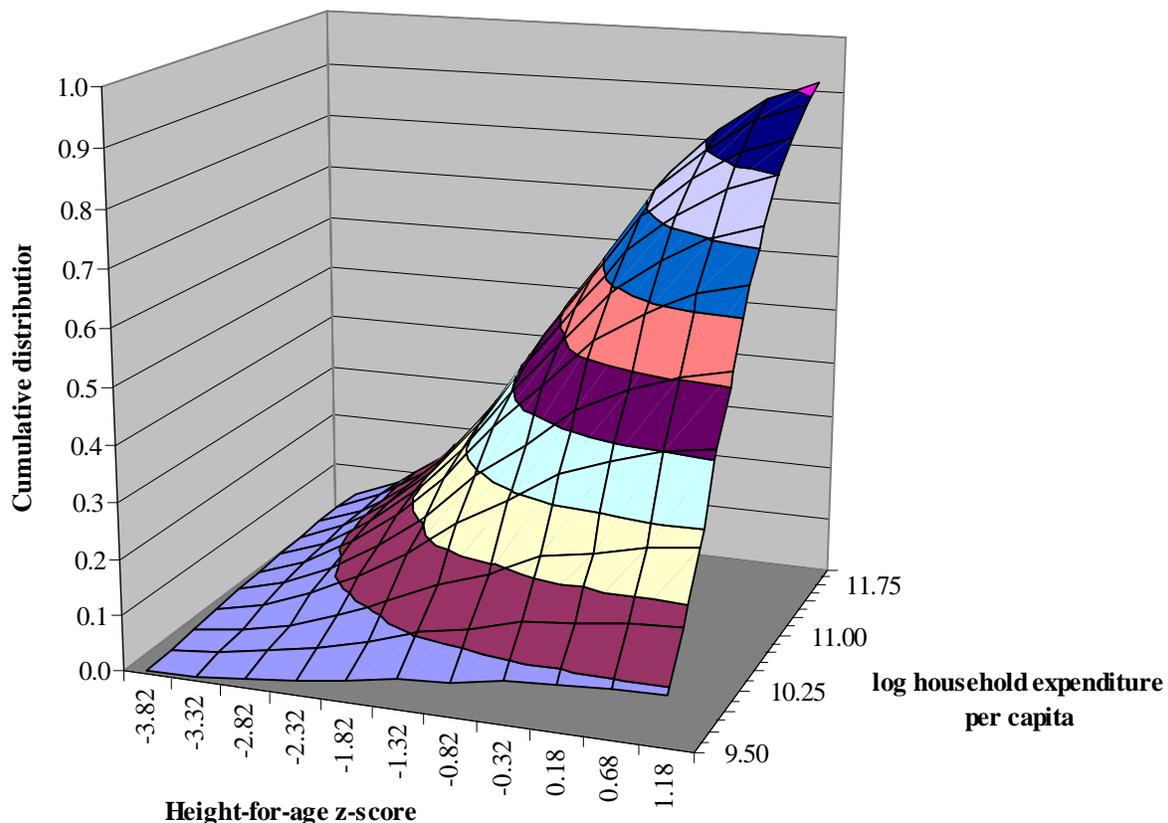
### ***2.3. Bivariate Poverty Dominance Methods***

Bivariate poverty dominance comparisons extend the univariate methods discussed above. If we have two measures of well-being rather than one, then Figure 1 becomes a three-dimensional graph, with one measure of well-being on the x-axis, a second on the y-axis, and the bivariate cdf on the z-axis (vertical), as in **Figure 3**. Note that the bivariate cdf is now a surface rather than a line, and we compare one cdf surface to another, just as in Figure 1. If one such surface is everywhere below another, then poverty in the first sample is lower than poverty in the second for a broad class of poverty measures, just as in the univariate case.

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<sup>12</sup> The transfer sensitivity principle says that if we make two symmetric but opposite transfers, one from a richer to a poorer person, and the other from a poorer to a richer person, with both of the latter being poorer than the participants in the first transfer, then poverty should decline (or not increase). The idea is that the social benefit of a transfer from a richer to a poorer person is larger the poorer are the two participants.

**Figure 3 - Bidimensional Poverty Dominance Surface**



That class, which we call  $\Pi^{1,1}$  to indicate that it is first-order in both dimensions of well-being, has characteristics analogous to those of the univariate case –non-decreasing in each dimension, anonymous – and one more, that the two dimensions of well-being be substitutes (or more precisely, not be complements) in the poverty measure. This means, roughly, that an increase of well-being in one dimension should have a greater effect on poverty the lower the level of well-being in the other dimension.<sup>13</sup> In most cases, this restriction is sensible: if we are able to improve a child’s health, for example, it seems ethically right that this should reduce overall poverty the most when the child is very poor in the income dimension. But there are some plausible exceptions. For example, suppose that only healthy children can learn in school. Then it might reduce poverty more if we concentrated health improvements on children who are in school (*better* off in the education dimension), because of the complementarity of health and education.

Practically, it is not easy to plot two surfaces such as the one in **Figure 3** on the same graph and see the differences between them, but we can plot the differences directly. If this difference always has the same sign, then we know that one or the other of the samples has lower poverty for a large class  $\Pi^{1,1}$  of poverty measures. If the surfaces cross, we can compare the distributions at higher orders of dominance, just as we did in the univariate case. This can be done in one or both dimensions of

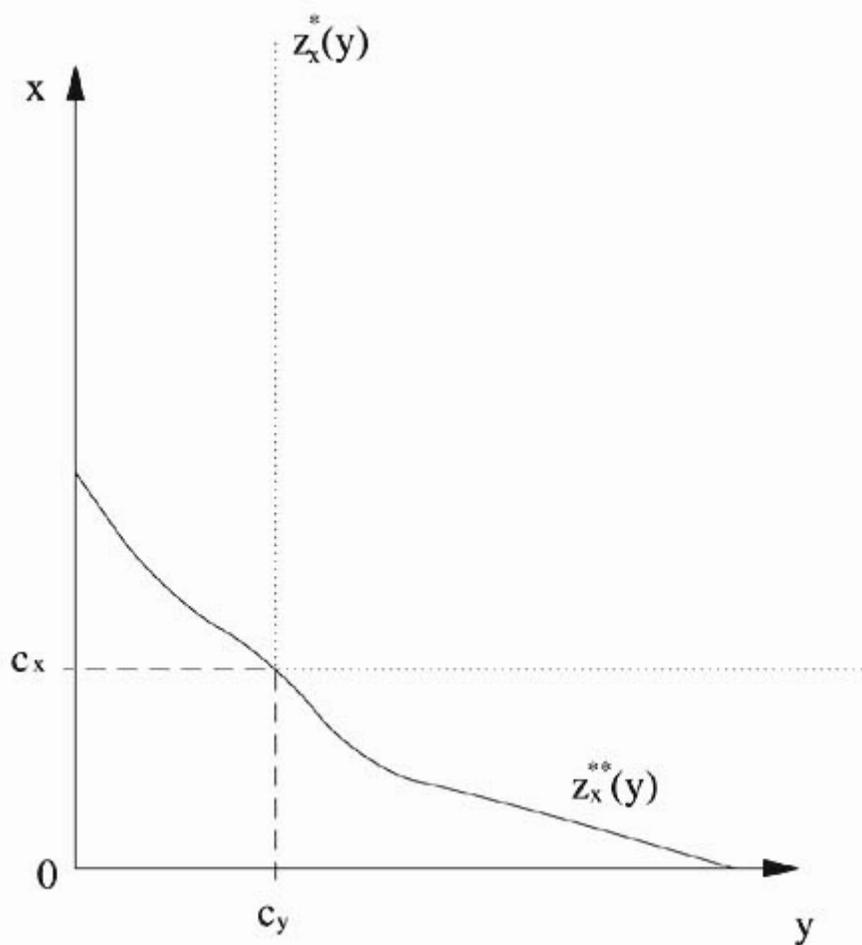
<sup>13</sup> Bourguignon and Chakravarty (2003) discuss this property in detail.

well-being, and the restrictions on the applicable classes of poverty measures are similar to the univariate case.

### Intersection, Union, and “Intermediate” Poverty Definitions

In addition to the extra conditions on the class of poverty indices, multivariate dominance comparisons require us to distinguish between union, intersection, and intermediate poverty measures. We can do this with the help of Figure 4, which shows the domain of dominance surfaces – the  $(x,y)$  plane. The function  $\lambda_1(x,y)$  defines an "intersection" poverty index: it considers someone to be in poverty only if she is poor in both of the dimensions  $x$  and  $y$ , and therefore if she lies within the dashed rectangle of Figure 4. The function  $\lambda_2(x,y)$  (the L-shaped, dotted line) defines a union poverty index: it considers someone to be in poverty if she is poor in *either* of the two dimensions, and therefore if she lies below or to the right of the dotted line. Finally,  $\lambda_3(x,y)$  provides an intermediate approach. Someone can be poor even if her  $y$  value is greater than the poverty line in the  $y$  dimension if her  $x$  value is sufficiently low to lie to the left of  $\lambda_3(x,y)$ .

**Figure 4 - Intersection, Union, and Intermediate Dominance Test Domains**



For one sample to have less intersection poverty than another, its dominance surface must be below the second sample's everywhere within an area like the one defined by  $\lambda_1(x,y)$ . To have less union poverty, its surface must be below the second sample's everywhere within an area like the one defined by  $\lambda_2(x,y)$ , and similarly for intermediate definitions and  $\lambda_3(x,y)$ . These are the sorts of comparisons that we will make in the applications that follow. Note, however, that if dominance is established for one of these areas, then it also necessarily obtains for any other sub-area, be it a union, intersection or intermediate one.

### Multivariate vs. Human Development Index Poverty Comparisons

Figure 4 is also helpful to understand the difference between the general multivariate poverty comparisons that we use here and comparisons that rely on indices created with multiple indicators of well-being, the best known of which is the Human Development Index (UNDP, 1990). An individual-level index of the x and y measures of well-being in Figure 4 might be written as

$$I = a_x x + a_y y$$

where  $a_x$  and  $a_y$  are some weights assigned to each variable. This index is now a univariate measure of well-being, and could be used for poverty comparisons such as those in Figure 1.<sup>14</sup> The domain of this test for such an index would follow roughly a ray starting at the origin and extending into the (x,y) plane at an angle that depends on the relative size of the weights  $a_x$  and  $a_y$ . Testing for dominance at these points only is clearly less general than tests over the entire area defined, for instance, by  $\lambda_1(x,y)$ ,  $\lambda_2(x,y)$ , or  $\lambda_3(x,y)$  in Figure 4.

**Table 1 -  $\Pi^{1,1}$  Dominance Tests for Rural and Urban areas in Toliara, Madagascar (differences between rural and urban dominance surfaces)**

|       |       |        |         |         |         |        |        |        |        |        |        |
|-------|-------|--------|---------|---------|---------|--------|--------|--------|--------|--------|--------|
|       | 16.51 | -8.841 | -16.320 | -16.580 | -11.430 | -8.068 | -6.658 | -4.174 | -2.208 | 0.022  | -0.239 |
|       | 13.19 | -9.286 | -16.780 | -16.090 | -11.080 | -7.815 | -6.221 | -3.662 | -0.933 | 2.005  | 2.118  |
|       | 12.84 | -9.845 | -15.690 | -15.930 | -10.720 | -7.053 | -5.253 | -2.017 | 1.018  | 3.969  | 4.288  |
|       | 12.60 | -3.307 | -11.960 | -9.174  | -3.734  | -0.638 | 1.677  | 5.642  | 8.312  | 11.250 | 11.090 |
|       | 12.44 | 1.646  | -10.230 | -7.667  | -2.467  | 0.711  | 3.174  | 7.454  | 10.100 | 13.360 | 13.260 |
| ln(y) | 12.29 | 1.263  | -6.159  | -3.925  | 1.479   | 5.464  | 7.136  | 10.410 | 12.260 | 16.550 | 15.620 |
|       | 12.16 | 0.628  | -3.287  | -2.195  | 2.421   | 5.733  | 7.625  | 12.410 | 14.220 | 18.720 | 17.440 |
|       | 12.00 | 6.766  | 4.360   | 6.195   | 10.920  | 14.140 | 15.600 | 19.430 | 21.820 | 26.530 | 27.180 |
|       | 11.82 | 7.153  | 4.561   | 4.882   | 8.766   | 12.440 | 13.510 | 15.620 | 17.350 | 22.040 | 22.570 |
|       | 11.48 | 5.048  | 1.268   | 1.683   | 7.348   | 10.780 | 11.660 | 13.610 | 14.920 | 16.750 | 17.340 |
|       | 0.000 | -4.01  | -3.33   | -2.84   | -2.39   | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|       |       | Haz    |         |         |         |        |        |        |        |        |        |

<sup>14</sup> The Human Development Index is actually cruder than this, as it first aggregates across individuals each dimension of well-being to generate a single scalar measure, and then constructs a weighted average of those scalars to generate the HDI, which is also a scalar.

**Table 1** gives an example of why our generalization of HDI-type univariate indices is important, comparing poverty in rural Toliara and urban Mahajanga/Antsiranana in Madagascar. The table shows the value of the t-statistic for a test of the difference in the two areas' poverty surfaces at a 10x10 grid of test points in a domain similar to Figure 4. We have highlighted the significantly negative differences in yellow (lighter in black-and-white) and the significantly positive differences in blue (darker in black-and-white). It is evidently possible to choose weights for an index composed of log household expenditures per capita and children's heights such that they ensure that we conclude that poverty is lower in urban Mahajanga/Antsiranana – this would take advantage of the test points that fit below the significantly negative tests in the upper left of the test domain. However, another set of weights would not permit the same conclusion and, in particular, more weight for expenditures would imply a significant crossing of the index's poverty incidence curves.

### Multivariate vs. Multiple Univariate Poverty Comparisons

Suppose that one conducts a univariate comparison between expenditures per capita in two samples, as in Figure 1, and children's heights in two samples, and finds that for both variables, one sample shows lower poverty for all poverty lines and a large class of poverty measures. Is that not sufficient to conclude that poverty differs in the two samples? Unfortunately, no. The complication comes from the “hump” in the middle of the dominance surface shown in **Figure 3**. How sharply the hump rises depends on the correlation between the two measures of well-being. If they are highly correlated, the surface rises rapidly in the center, and vice-versa. Thus, it is possible for one surface to be lower than another at both extremes (the edges of the surface farthest from the origin) and yet higher in the middle if the correlation between the welfare variables is higher. The far edges of each surface integrate out one variable, and so are the univariate cdf's depicted in Figure 1. Thus, in this case, one surface would have lower univariate cdf's, and thus lower poverty, for both measures of well-being independently, but it would not have lower bivariate poverty. Intuitively, samples with higher correlation of deprivation in multiple dimensions have higher poverty than samples with lower correlation because lower well-being in one dimension contributes more to poverty if well-being is also low in the other dimension.

**Table 2 -  $\Pi^{1,1}$  Dominance Tests for Rural Central vs. Urban Eastern Regions, Uganda**

|       |        |        |        |        |        |        |        |        |        |        |        |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|       | 11.660 | 2.637  | 12.510 | 8.720  | 7.938  | 9.993  | 7.941  | 11.170 | 4.484  | 1.109  | 0.000  |
|       | 9.276  | 3.458  | 13.930 | 9.712  | 12.030 | 15.540 | 15.410 | 20.020 | 13.550 | 14.130 | 16.400 |
|       | 8.996  | 5.519  | 14.940 | 10.590 | 13.920 | 17.110 | 17.110 | 22.360 | 18.330 | 18.410 | 20.250 |
|       | 8.803  | 2.559  | 11.910 | 7.156  | 10.320 | 13.760 | 14.730 | 21.160 | 18.730 | 19.030 | 21.460 |
|       | 8.664  | 0.610  | 8.643  | 4.224  | 7.651  | 9.988  | 9.820  | 15.270 | 15.010 | 16.430 | 19.950 |
| ln(y) | 8.527  | 0.062  | 8.763  | 5.016  | 8.366  | 9.201  | 12.340 | 17.300 | 15.860 | 17.390 | 19.570 |
|       | 8.395  | -2.842 | 5.754  | -0.025 | 2.692  | 4.249  | 6.958  | 10.650 | 12.260 | 13.580 | 15.240 |
|       | 8.249  | -1.582 | 5.582  | -0.307 | 2.743  | 2.801  | 5.305  | 8.590  | 11.310 | 13.020 | 13.520 |
|       | 8.068  | -4.756 | 1.731  | -4.960 | -1.046 | 0.140  | 2.003  | 4.765  | 6.872  | 9.221  | 8.636  |
|       | 7.824  | 4.698  | 8.001  | 8.184  | 9.695  | 7.846  | 10.090 | 12.120 | 12.850 | 13.900 | 12.290 |
|       | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|       |        |        |        |        |        |        |        |        |        |        | Haz    |

Table 2 provides an example. Univariate poverty is unambiguously higher in rural Central region than urban Eastern region in *both* dimensions, yet bivariate poverty is not, because of the statistically significant reversal of the dominance surfaces in the interior. Even at higher orders up to  $s_x=3$  and  $s_y=3$  we find that the dominance surfaces cross for these two areas.

It is also possible that two samples with different correlations between measures of well-being have univariate comparisons that are inconclusive – they cross at the extreme edges of the dominance surfaces – but have bivariate surfaces that are different for a large part of the interior of the dominance surface. (The sample with lower correlation would have a lower dominance surface). This would establish different intersection multivariate poverty even though either one or both of the univariate comparisons is inconclusive. It could not, however, establish union poverty dominance, since that requires difference in the surfaces at the extremes as well as in the middle.

**Table 3 -  $\Pi^{2,2}$  Dominance Tests for Rural Central and Urban Northern Regions, Uganda**

|       |        |         |         |         |         |         |         |         |        |        |        |
|-------|--------|---------|---------|---------|---------|---------|---------|---------|--------|--------|--------|
|       | 11.660 | -0.824  | 0.263   | 1.863   | 1.217   | 0.048   | -1.722  | -2.680  | -3.454 | -3.200 | -0.497 |
|       | 9.276  | -6.401  | -5.347  | -4.431  | -4.999  | -5.578  | -6.354  | -6.607  | -6.573 | -5.397 | -0.773 |
|       | 8.996  | -7.860  | -6.909  | -6.315  | -6.911  | -7.340  | -7.700  | -7.669  | -7.393 | -6.083 | -1.396 |
|       | 8.803  | -9.091  | -8.169  | -7.775  | -8.286  | -8.554  | -8.556  | -8.240  | -7.784 | -6.395 | -1.564 |
|       | 8.664  | -10.090 | -9.240  | -8.997  | -9.437  | -9.571  | -9.347  | -8.833  | -8.222 | -6.765 | -1.849 |
| ln(y) | 8.527  | -10.750 | -10.000 | -9.823  | -10.120 | -10.080 | -9.603  | -8.851  | -8.014 | -6.456 | -1.365 |
|       | 8.395  | -11.190 | -10.360 | -10.100 | -10.310 | -10.300 | -9.793  | -8.981  | -8.069 | -6.595 | -1.725 |
|       | 8.249  | -11.820 | -11.280 | -10.990 | -11.140 | -11.190 | -10.810 | -10.140 | -9.274 | -7.970 | -3.535 |
|       | 8.068  | -12.150 | -11.680 | -11.270 | -11.130 | -11.010 | -10.610 | -9.910  | -8.959 | -7.705 | -3.469 |
|       | 7.824  | -12.240 | -11.870 | -11.450 | -11.040 | -10.650 | -10.210 | -9.528  | -8.628 | -7.559 | -4.168 |
|       | 0.000  | -3.100  | -2.450  | -1.970  | -1.580  | -1.220  | -0.880  | -0.500  | -0.010 | 0.690  | 5.820  |
|       |        |         |         |         |         |         |         |         |        |        | Haz    |

Table 3 gives an example. Here, there is no statistically significant univariate dominance in the expenditure dimension of well-being, but there is a sizeable domain – up to the ninth decile in each dimension – over which poverty is lower in rural Central region than in urban Northern region for all intersection poverty indices in the  $\Pi^{2,2}$  class.

### 3. Bivariate Spatial Poverty Comparisons in Africa

In this section, we apply bivariate dominance tests to the question of spatial poverty comparisons in Ghana, Madagascar, and Uganda. We compare poverty in urban and rural areas, nationally and by region, measured in terms of household expenditures per capita and children’s height-for-age z-scores. The tests produce a large amount of output in the form of tables such as

Table 1, which we relegate to appendices. Here, we report summaries of the dominance results.

Table 4 gives descriptive statistics for height-for-age z-scores (HAZ) and the log of household expenditures per capita (ln(y)). As one would expect, poverty measured by expenditures per capita

and also stunting<sup>15</sup> are higher in rural than urban areas in each country. The same is true within each region of each country, except for Toliara region in Madagascar, where stunting is higher in urban than in rural areas. In fact, with a few exceptions in Madagascar, both expenditure and height poverty are lower in urban areas in any region than in rural areas in any other.

In addition to the means and poverty rates, Table 4 also reports the correlation between the log of expenditures per capita and height-for-age z-scores. Note that in Uganda and Madagascar expenditures and heights are more highly correlated in urban than rural areas, while both expenditures and heights tend to be higher in urban areas. As noted above, this combination can cause bivariate poverty comparisons to differ from univariate comparisons carried out separately in each dimension of well-being.

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<sup>15</sup> Stunting usually is defined as a height-for-age z-score of less than  $-2$ .

**Table 4- Descriptive Statistics for Poverty and Stunting**

| Region            | Area  | Mean  |       | Percent |      | N    | Correlation<br>ln(y),HAZ |
|-------------------|-------|-------|-------|---------|------|------|--------------------------|
|                   |       | HAZ   | ln(y) | Stunted | Poor |      |                          |
| <b>Ghana</b>      |       |       |       |         |      |      |                          |
| Coast             |       | -0.98 | 11.90 | 0.22    | 0.41 | 911  | 0.15                     |
|                   | Rural | -1.12 | 11.76 | 0.27    | 0.51 | 488  | 0.10                     |
|                   | Urban | -0.82 | 12.06 | 0.16    | 0.30 | 423  | 0.15                     |
| Forest            |       | -1.38 | 11.81 | 0.32    | 0.46 | 1074 | 0.12                     |
|                   | Rural | -1.48 | 11.79 | 0.35    | 0.48 | 793  | 0.11                     |
|                   | Urban | -1.10 | 11.88 | 0.24    | 0.39 | 281  | 0.10                     |
| Savannah          |       | -1.30 | 11.66 | 0.32    | 0.55 | 683  | 0.11                     |
|                   | Rural | -1.37 | 11.63 | 0.33    | 0.56 | 591  | 0.13                     |
|                   | Urban | -0.86 | 11.85 | 0.23    | 0.48 | 92   | -0.08                    |
| National          |       | -1.22 | 11.80 | 0.28    | 0.47 | 2668 | 0.14                     |
|                   | Rural | -1.35 | 11.73 | 0.32    | 0.51 | 1872 | 0.11                     |
|                   | Urban | -0.92 | 11.97 | 0.19    | 0.35 | 796  | 0.11                     |
| <b>Madagascar</b> |       |       |       |         |      |      |                          |
| Tana              |       | -2.24 | 12.32 | 0.57    | 0.73 | 928  | 0.26                     |
|                   | Rural | -2.33 | 12.26 | 0.60    | 0.78 | 534  | 0.25                     |
|                   | Urban | -1.80 | 12.65 | 0.40    | 0.48 | 394  | 0.20                     |
| Fian/Toa          |       | -2.15 | 12.26 | 0.53    | 0.77 | 975  | 0.03                     |
|                   | Rural | -2.19 | 12.22 | 0.54    | 0.80 | 705  | 0.00                     |
|                   | Urban | -1.74 | 12.56 | 0.48    | 0.56 | 270  | 0.17                     |
| Maha/Antsi        |       | -1.35 | 12.62 | 0.34    | 0.55 | 561  | -0.02                    |
|                   | Rural | -1.32 | 12.61 | 0.34    | 0.56 | 346  | -0.04                    |
|                   | Urban | -1.44 | 12.71 | 0.34    | 0.50 | 215  | 0.14                     |
| Toliara           |       | -1.91 | 12.06 | 0.48    | 0.78 | 457  | -0.18                    |
|                   | Rural | -1.82 | 11.98 | 0.45    | 0.82 | 302  | -0.19                    |
|                   | Urban | -2.36 | 12.46 | 0.60    | 0.57 | 155  | 0.02                     |
| National          |       | -1.97 | 12.33 | 0.50    | 0.71 | 2921 | 0.07                     |
|                   | Rural | -2.01 | 12.27 | 0.51    | 0.75 | 1887 | 0.05                     |
|                   | Urban | -1.79 | 12.61 | 0.44    | 0.52 | 1034 | 0.17                     |
| <b>Uganda</b>     |       |       |       |         |      |      |                          |
| Central           |       | -1.00 | 8.80  | 0.25    | 0.19 | 1806 | 0.07                     |
|                   | Rural | -1.08 | 8.65  | 0.27    | 0.23 | 1390 | 0.04                     |
|                   | Urban | -0.77 | 9.22  | 0.18    | 0.08 | 416  | 0.03                     |
| Eastern           |       | -1.22 | 8.48  | 0.28    | 0.38 | 2349 | 0.09                     |
|                   | Rural | -1.25 | 8.45  | 0.28    | 0.39 | 2010 | 0.06                     |
|                   | Urban | -0.75 | 8.99  | 0.21    | 0.14 | 339  | 0.21                     |
| Western           |       | -1.42 | 8.63  | 0.34    | 0.28 | 2096 | 0.12                     |
|                   | Rural | -1.46 | 8.60  | 0.35    | 0.29 | 1860 | 0.07                     |
|                   | Urban | -0.59 | 9.35  | 0.15    | 0.06 | 236  | 0.25                     |
| Northern          |       | -1.24 | 8.16  | 0.30    | 0.60 | 1230 | 0.09                     |
|                   | Rural | -1.24 | 8.13  | 0.30    | 0.62 | 1008 | 0.08                     |
|                   | Urban | -1.23 | 8.72  | 0.26    | 0.19 | 222  | 0.36                     |
| National          |       | -1.22 | 8.54  | 0.29    | 0.35 | 7481 | 0.10                     |
|                   | Rural | -1.27 | 8.47  | 0.30    | 0.37 | 6268 | 0.06                     |
|                   | Urban | -0.79 | 9.15  | 0.19    | 0.10 | 1213 | 0.12                     |

Table 5 through Table 7 summarize the dominance results for tests across urban and rural areas in Ghana, Madagascar, and Uganda. For each country as a whole, poverty is higher in rural than urban areas for each univariate poverty comparison (columns 3 and 4) and for both intersection and union bivariate comparisons (columns 5 and 6). These results are entirely consistent with virtually every poverty comparison that we know of based on incomes or expenditures alone – poverty is lower in urban areas.

In the regional comparisons, however, a significant number of exceptions to this widely held belief emerge, especially for the bivariate comparisons. Ghana has the fewest of these, with two of nine urban-rural comparisons being statistically insignificant for both intersection and union bivariate poverty comparisons. In Uganda, four of sixteen intersection and union comparisons cannot reject the null of non dominance, and two of these – rural areas in Eastern and Western region vs. urban areas in Northern region – actually have somewhat limited domains over which bivariate poverty is lower in the rural area for intersection poverty measures. In Madagascar, seven of sixteen intersection comparisons and ten of sixteen union comparisons cannot reject the null that bivariate poverty is the same in urban and rural areas, though none of these reject the null in favor of rural areas. Overall, then, the proposition that poverty is always higher in rural areas than urban areas does not get the same overwhelming support in these results that it almost always does in univariate poverty comparisons in Africa.

One immediate concern with these results is that the interesting cases are ones in which we are not rejecting the null of non-dominance, so they may be driven by a lack of power in the statistical tests. This concern is reinforced by the relatively few observations that are available in some urban areas. Review of the appendices shows, however, that in most of the cases in which we do not find bivariate dominance, the dominance surfaces actually cross significantly. That is, there are points in the test domain where the rural surface is significantly above the urban surface and vice-versa. We have noted these cases in the last column of Table 5 through Table 7 for first-order comparisons in both dimensions. Thus, the lack of bivariate dominance is typically not due to a lack of power.

To gain a better understanding of how bivariate and univariate dominance methods can differ, we classify the results into five types. For type 1, we have dominance (usually first-order) for both univariate comparisons and for intersection and union bivariate comparisons. This is the most common result, accounting for 25 of the 41 comparisons. This is also the least interesting type of result for our methods, because one could ask “why bother with the more complicated bivariate comparisons if, in the end, they produce the same results as simpler univariate dominance tests, or even scalar comparisons?”

Type 2 is equally uninteresting for our methods. This occurs when neither the univariate nor the bivariate methods finds dominance. Fortunately, there is only one such case, for urban and rural Mahajanga/Antsiranana region in Madagascar.

Type 3 is a case in which urban areas dominate rural for both univariate comparisons but not for the bivariate comparisons. There are six of these cases. There is also one case, rural Mahajanga/Antsirana vs. urban Toliara, in which the *rural* area dominates on both univariate comparisons, but not in the bivariate comparisons. For cases in which the bivariate comparisons are inconsistent with the univariate comparisons, a type 3 result is the most common. The bivariate

comparisons are more demanding than univariate comparisons, so it makes sense that they reject the null of non-dominance less often, and this happens in five of the seven cases. In two, both involving urban areas in the Northern region of Uganda, the dominance result is actually reversed for intersection poverty measures over a limited domain. This is quite surprising, but understandable once we observe the very high correlation (0.36) between expenditures and heights in urban Northern region compared to rural Western and Eastern regions (0.07 and 0.06, respectively. See Table 4.)

Type 4 occurs when the univariate results are contradictory in the sense that we find univariate dominance in one dimension but not the other. There are six such occurrences, and in all but one we find that the urban area dominates in one dimension, usually expenditures, although there is one case, rural Central vs. urban Northern regions in Uganda, in which the rural area dominates, albeit only for the  $\Pi^3$  class. Of these six cases, we find intersection dominance for four bivariate tests. That is, the bivariate tests are able to “resolve” the conflicting univariate results for at least some classes of poverty measures<sup>16</sup> and areas of poverty lines.

Type 5 is similar to type 4 except that the contradictory univariate results are statistically significant in each univariate comparison. There are only two of these cases, rural vs. urban Toliara, and rural Coast vs. urban Forest in Ghana. Unlike the type 4 results, in neither case are any of the bivariate poverty comparisons statistically significant, so the bivariate comparisons cannot resolve the univariate conflict.

Overall, we certainly have not amassed sufficient evidence to overturn the standard presumption that poverty is lower in urban than in rural areas, but enough of our results are at odds with this idea to give us pause. Further, we have seen that the reasons that we do not find this for bivariate poverty comparisons vary. For the type 4 and 5 cases, we find no univariate dominance in one dimension or another, and the bivariate results follow from that. But this is relatively rare, and in about half of these cases the bivariate tests for intersection poverty measures do actually find that poverty is lower in urban areas despite the contradictory univariate results. Most of the differences, though, come from the fact that our two measures of well-being are often more highly correlated in urban areas than in rural areas. As noted above, this correlation causes the poverty incidence surface to rise more rapidly near the origin of the distribution, raising it above the rural surface in the center even though it is below it at the extremes where we find the univariate poverty incidence curves. In most cases, this gives us results in which an urban area dominates a rural area in each dimension individually, but not jointly, because multiple deprivation is more common in urban areas. There are two cases, however, in which the dominance is actually reversed, so that for some intersection poverty measures, the rural area actually dominates the urban.

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<sup>16</sup> As noted in the methods discussion, bivariate dominance for union poverty measures requires univariate dominance in each dimension, so it is impossible for this type of result.

**Table 5 - Summary of Dominance Tests for Ghana**

| Rural    | Urban       | Univariate               | HAZ        | Bivariate    | Union                      | Crossing? |
|----------|-------------|--------------------------|------------|--------------|----------------------------|-----------|
|          |             | ln(y)                    |            | Intersection |                            |           |
|          | National    | U d. R (1)               | U d. R (1) | U d. R (1,1) | U d. R (1,1)               |           |
| Region:  | vs. Region: |                          |            |              |                            |           |
| Coast    | Coast       | U d. R (1)               | U d. R (1) | U d. R (1,1) | U d. R (1,1)               |           |
|          | Forest      | U d. R (1)               | R d. U (2) | none         | none                       | yes       |
|          | Savannah    | U d. R (2)               | U d. R (2) | U d. R (2,2) | U d. R (2,2)               |           |
| Forest   | Coast       | U d. R (1)               | U d. R (1) | U d. R (1,1) | U d. R (1,1)               |           |
|          | Forest      | U d. R (1) <sup>1/</sup> | U d. R (1) | none         | none                       | no        |
|          | Savannah    | U d. R (1)               | U d. R (2) | U d. R (1,1) | U d. R (2,2)               |           |
| Savannah | Coast       | U d. R (1)               | U d. R (1) | U d. R (1,1) | U d. R (1,1)               |           |
|          | Forest      | U d. R (1)               | U d. R (1) | U d. R (1,1) | U d. R (1,1) <sup>2/</sup> |           |
|          | Savannah    | U d. R (1)               | U d. R (2) | U d. R (1,1) | U d. R (2,2)               |           |

Notes: “A d. B” means that poverty in A is lower than in B for all reasonable poverty lines. The order of dominance is given in parentheses. For the bivariate comparisons, the first entry is for the height-for-age z-score, and the second is for the dimension of log of household expenditures per capita.

<sup>1/</sup>One test point is significant only at the 10% level.

<sup>2/</sup>Two test points are significant only at the 10% level.

**Table 6 - Summary of Dominance Tests for Madagascar**

| Rural      | Urban      | Univariate | Bivariate  |                            |                            | Crossing? |
|------------|------------|------------|------------|----------------------------|----------------------------|-----------|
|            |            | ln(y)      | HAZ        | Intersection               | Union                      |           |
|            | National   | U d. R (1) | U d. R (1) | U d. R (1,1) <sup>1/</sup> | U d. R (1,1) <sup>1/</sup> |           |
| Rural:     | vs. Urban: |            |            |                            |                            |           |
| Tana       | Tana       | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1)               |           |
|            | Fian/Tao   | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) <sup>1/</sup> |           |
|            | Maha/Antsi | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1)               |           |
|            | Toliara    | U d. R (1) | none       | U d. R (2,2)               | none                       | yes       |
| Fian/Tao   | Tana       | U d. R (1) | U d. R (1) | none                       | none                       | no        |
|            | Fian/Tao   | U d. R (1) | U d. R (1) | none                       | none                       | no        |
|            | Maha/Antsi | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) <sup>2/</sup> |           |
|            | Toliara    | U d. R (1) | none       | U d. R (2,2)               | none                       | yes       |
| Maha/Antsi | Tana       | U d. R (2) | U d. R (1) | U d. R (2,2) <sup>1/</sup> | U d. R (2,2) <sup>1/</sup> |           |
|            | Fian/Tao   | none       | U d. R (1) | U d. R (2,2)               | none                       | yes       |
|            | Maha/Antsi | none       | none       | none                       | none                       | yes       |
|            | Toliara    | R d. U (1) | R d. U (2) | none                       | none                       | yes       |
| Toliara    | Tana       | U d. R (1) | none       | none                       | none                       | no        |
|            | Fian/Tao   | U d. R (1) | none       | none                       | none                       | yes       |
|            | Maha/Antsi | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1)               |           |
|            | Toliara    | R d. U (1) | U d. R (1) | none                       | none                       | yes       |

Notes: “A d. B” means that poverty in A is lower than in B for all reasonable poverty lines. The order of dominance is given in parentheses. For the bivariate comparisons, the first entry is for the height-for-age z-score, and the second is for the dimension of log of household expenditures per capita.

<sup>1/</sup>One test point is significant only at the 10% level.

<sup>2/</sup>One test point is significant only at the 10% level, and one is insignificant.

**Table 7 - Summary of Dominance Tests for Uganda**

| Rural    | Urban       | Univariate | Bivariate  |                            |              | Crossing? |
|----------|-------------|------------|------------|----------------------------|--------------|-----------|
|          |             | ln(y)      | HAZ        | Intersection               | Union        |           |
|          | National    | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
| Region:  | vs. Region: |            |            |                            |              |           |
| Central  | Central     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Eastern     | U d. R (1) | U d. R (1) | none                       | none         | yes       |
|          | Western     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
| Eastern  | Northern    | R d. U (3) | none       | R d. U (2,2)               | none         | yes       |
|          | Central     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Eastern     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
| Western  | Western     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Northern    | U d. R (1) | U d. R (2) | R d. U (ltd) <sup>1/</sup> | none         | yes       |
|          | Central     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
| Northern | Eastern     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Western     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Northern    | U d. R (1) | U d. R (2) | R d. U (ltd) <sup>1/</sup> | none         | yes       |
| Northern | Central     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Eastern     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Western     | U d. R (1) | U d. R (1) | U d. R (1,1)               | U d. R (1,1) |           |
|          | Northern    | U d. R (1) | U d. R (2) | U d. R (1,1)               | U d. R (2,2) |           |

Notes: “A d. B” means that poverty in A is lower than in B for all reasonable poverty lines. The order of dominance is given in parentheses. For the bivariate comparisons, the first entry is for the dimension of log of household expenditures per capita, and the second is for the height-for-age z-score.

<sup>1/</sup>Dominance is limited to a relatively small domain of poverty frontiers in  $\Pi^{2,2}$ , and a larger one in  $\Pi^{3,3}$ .

## Conclusions

This paper has used bivariate stochastic dominance techniques to compare poverty in urban vs. rural areas in three African countries, where poverty is measured in terms of expenditures per capita and children's standardized heights, a good measure of children's health status. We have shown that our comparisons are more general than either a comparison of a Human Development-type index or "one-at-a-time" comparisons of multiple measures of well-being. More importantly, we find that our more general methods are at odds with simpler univariate poverty comparisons in a non-trivial number of cases.

Expenditure-based urban-rural poverty comparisons almost always find that rural areas are poorer than urban. Our results are consistent with that finding whether we use univariate or bivariate comparisons. However, differences emerge when we compare urban areas in one region of a country with rural areas in another region. We find several cases in which univariate poverty is lower in urban areas in both dimensions, but bivariate poverty is not. This happens because the correlation between expenditures per capita and children's heights is higher in the urban areas, so that urban residents who are expenditure poor are more likely also to be health poor. This correlation yields a higher density of observations in the poorest part of the bivariate welfare domain for urban areas, even though there are fewer observations for urban residents at the lower end of the density for each individual measure of well-being. We believe that taking such a correlation into account is important for welfare comparisons because the social cost of poverty in one dimension, say health, is higher if the person affected is also poor in the other dimension (expenditures).

It is interesting to note that the share of cases in which urban areas do not dominate rural is much higher in our bivariate comparisons than it is for expenditure- or income-based comparisons in the existing literature. In addition, we hasten to add that with two exceptions, both in Madagascar, the urban area in the region where the capital is located always dominates every rural area in both univariate and bivariate comparisons.

There are other instances in which our bivariate comparisons are at odds with univariate comparisons. Perhaps the most interesting are cases in which univariate results are inconclusive because one or the other univariate comparison is inconclusive, yet the bivariate results find dominance for a large domain of intersection poverty indices. This arises in about 10 percent of our examples and occurs again when the correlation between expenditures per capita and children's heights differs significantly across areas. These results are interesting because they show that bivariate comparisons may actually provide statistically significant results when univariate comparisons do not.

Hence, the finding that bivariate results often differs from the standard perception of greater rural poverty is typically not because children are taller in rural areas, but rather because the correlation between expenditures and heights is lower there than in urban areas. This, however, is based on only three countries: pursuing similar research in other countries will yield insight as to whether these results are anomalous. Why this should be is also an interesting question for future research. But a clear implication of these results for researchers and policy makers interested in multiple

dimensions of poverty is that, at a minimum, one should check the correlations between measures of well-being in the groups of interest. Large differences in these correlations may lead to unexpected multivariate dominance comparisons.

## Bibliography

- Atkinson, A.B. (2003). "Multidimensional Deprivation: Contrasting Social Welfare and Counting Approaches", *The Journal of Economic Inequality* **1**(1), 51-65.
- Atkinson, A.B. (1987). "On the Measurement of Poverty," *Econometrica*, **55**, 749-764.
- Atkinson, A.B. and F. Bourguignon (1982). "The Comparison of Multi-Dimensional Distributions of Economic Status," chapter 2 in *Social Justice and Public Policy*, Harvester Wheatsheaf, London.
- Atkinson, A.B. and F. Bourguignon (1987). "Income Distribution and Differences in Needs," in G.R. Feiwel, ed., *Arrow and the foundations of the theory of economic policy*, New York Press, New York, 350-70.
- Appleton, Simon, 2000. "Poverty in Uganda, 1999/2000:Preliminary estimates from the UNHS," mimeo, Uganda Bureau of Statistics.
- Appleton, Simon, 2001, "Poverty reduction during growth: the case of Uganda, 1992-2000," mimeo.
- Appleton, Simon, Song, Lina (1999). *Income and Human Development at the Household Level: Evidence from Six Countries*, Mimeo, University of Oxford: Centre for the Study of African Economies.
- Beaton, G. H. et al. 1990. *Appropriate uses of anthropometric indices in children: a report based on an ACC/SCN workshop*. United Nations Administrative Committee on Coordination/Subcommittee on Nutrition (ACC/SCN State-of-the-Art Series, Nutrition Policy Discussion Paper No. 7), New York.
- Bourguignon, F., and S. R. Chakravarty (2003). "The measurement of multidimensional poverty," *The Journal of Economic Inequality* **1**(1), 25-49.
- Bourguignon, F. and S.R. Chakravarty, (2002). "Multi-dimensional poverty orderings", DELTA, Paris.
- Cole, T. J., Parkin, J. M. 1977. Infection and its effect on growth of young children: A comparison of the Gambia and Uganda. *Transactions of the Royal Society of Tropical Medicine and Hygiene* **71**, 196-198.
- Crawford, Ian A. (1999). "Nonparametric Tests of Stochastic Dominance in Bivariate Distributions, with an Application to UK", University College London Discussion Papers in Economics 99/07.
- Davidson, R. and J.-Y. Duclos (2000). "Statistical Inference for Stochastic Dominance and the for the Measurement of Poverty and Inequality," *Econometrica*, **68**, 1435--1465.

- Duclos, J.-Y. and P. Makdissi (1999), "Sequential Stochastic Dominance and the Robustness of Poverty Orderings", Cahier de recherche 99-05, CRÉFA, Département d'économie, Université Laval.
- Duclos, J.-Y. and P. Makdissi (2000). "Sequential Stochastic Dominance and the Robustness of Poverty Orderings," Cahier de recherche, Département économique, Université Laval.
- Duclos, Jean-Yves, David Sahn, and Stephen D. Younger, 2003, "Robust Multidimensional Poverty Comparisons," Cornell Food and Nutrition Policy Program, working paper #98.
- Foster, J.E., (1984). "On Economic Poverty: A Survey of Aggregate Measures", in R.L. Basmann and G.F. Rhodes, eds., *Advances in Econometrics*, **3**, Connecticut: JAI Press, p. 215-251.
- Foster, J.E., J. Greer and E. Thorbecke (1984). "A Class of Decomposable Poverty Measures," *Econometrica*, **52** (3), 761--776.
- Foster, J.E. and A.F. Shorrocks (1988a). "Poverty Orderings," *Econometrica*, **56**, 173--177.
- Foster, J.E. and A.F. Shorrocks (1988b). "Poverty Orderings and Welfare Dominance," *Social Choice Welfare*, **5**, 179--198.
- Foster, J.E. and A.F. Shorrocks (1988c). "Inequality and Poverty Orderings," *European Economic Review*, **32**, 654--662.
- Mosley, W. H., Chen, L. C. 1984. An analytical framework for the study of child survival in developing countries. *Population and Development Review* 10(Supplement): 25-45.
- Pradhan, Menno, David E. Sahn, and Stephen D. Younger (2003). "Decomposing World Health Inequality," *Journal of Health Economics*, **22**, 271-293.
- Ravallion, Martin, and Benu Bidani, 1994, "How Robust is a Poverty Profile?" *World Bank Economic Review* **8**(1): 75-102.
- Shorrocks, A.F., and J. Foster (1987). "Transfer Sensitive Inequality Measures", *Review of Economic Studies*, **54**, 485--497.
- Tsui, K, (2002). "Multidimensional poverty indices", *Social Choice and Welfare*, **19** 69--93.
- United Nations Development Program (1990). *Human Development Report*. New York: Oxford University Press.
- World Health Organization. 1983. *Measuring Change in Nutritional Status: Guidelines for Assessing the Nutritional Impact of Supplementary Feeding Programmes for Vulnerable Groups*. WHO, Geneva.

World Health Organization (WHO) 1995. An evaluation of infant growth: the use and interpretation of anthropometry in infants. *Bulletin of the World Health Organization* 73, 165-174.

**Table A. 1 -  $\Pi^{1,1}$  Dominance Tests for Rural and Urban Areas in Ghana**

|       |       |       |       |       |       |       |       |       |       |       |       |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|       | 13.66 | 6.49  | 9.41  | 9.16  | 6.26  | 5.55  | 6.00  | 4.87  | 2.60  | 1.21  | 0.12  |
|       | 12.51 | 6.73  | 9.61  | 10.17 | 7.66  | 6.94  | 7.78  | 7.31  | 5.31  | 4.43  | 4.02  |
|       | 12.27 | 6.15  | 9.08  | 9.79  | 7.46  | 7.16  | 7.98  | 7.62  | 6.37  | 5.75  | 5.29  |
|       | 12.09 | 6.48  | 10.29 | 11.06 | 8.48  | 8.44  | 9.73  | 9.59  | 9.00  | 8.65  | 8.42  |
|       | 11.96 | 7.42  | 10.40 | 11.18 | 9.13  | 8.84  | 9.99  | 9.92  | 9.90  | 9.45  | 8.98  |
| ln(y) | 11.81 | 8.37  | 10.93 | 12.02 | 10.06 | 9.97  | 11.01 | 11.13 | 11.22 | 10.45 | 9.77  |
|       | 11.67 | 7.85  | 9.35  | 11.34 | 9.58  | 10.25 | 10.82 | 11.11 | 11.01 | 10.58 | 10.25 |
|       | 11.51 | 7.18  | 8.53  | 10.48 | 9.17  | 9.52  | 10.56 | 10.96 | 11.06 | 10.83 | 10.38 |
|       | 11.31 | 5.02  | 5.94  | 8.12  | 7.20  | 6.91  | 7.10  | 7.44  | 7.44  | 7.39  | 7.30  |
|       | 11.07 | 5.22  | 4.91  | 6.61  | 6.00  | 6.74  | 6.70  | 7.58  | 6.83  | 6.94  | 7.39  |
|       | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
|       |       |       |       |       |       |       |       |       |       |       | HAZ   |

**Table A. 2 -  $\Pi^{1,1}$  Dominance Tests for Rural Coast vs. Urban Areas in Ghana**

| Urban Coast    |       |       |       |       |       |       |       |       |       |       |       |
|----------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|                | 13.66 | 6.47  | 8.03  | 8.19  | 5.97  | 4.91  | 5.58  | 5.02  | 2.08  | -0.84 | 0.17  |
|                | 12.51 | 5.16  | 7.60  | 8.30  | 6.91  | 6.11  | 7.23  | 7.46  | 4.94  | 2.77  | 4.55  |
|                | 12.27 | 5.20  | 8.65  | 8.93  | 7.92  | 8.52  | 9.76  | 10.15 | 8.64  | 6.86  | 8.69  |
|                | 12.09 | 5.37  | 9.41  | 10.52 | 9.27  | 9.83  | 11.53 | 12.40 | 11.64 | 10.31 | 12.35 |
|                | 11.96 | 6.53  | 10.05 | 11.19 | 10.19 | 10.52 | 11.64 | 13.13 | 13.00 | 11.38 | 13.20 |
| ln(y)          | 11.81 | 8.13  | 10.14 | 11.23 | 9.27  | 9.97  | 11.11 | 12.10 | 12.57 | 10.90 | 12.02 |
|                | 11.67 | 7.25  | 8.51  | 10.12 | 9.18  | 10.16 | 10.71 | 12.34 | 12.70 | 11.82 | 13.22 |
|                | 11.51 | 6.99  | 9.18  | 10.58 | 9.96  | 11.06 | 11.92 | 13.15 | 12.90 | 12.17 | 13.26 |
|                | 11.31 | 3.79  | 5.71  | 7.37  | 7.39  | 7.81  | 7.39  | 8.71  | 8.30  | 7.95  | 9.03  |
|                | 11.07 | 3.61  | 2.99  | 4.45  | 4.18  | 4.58  | 3.87  | 6.12  | 5.32  | 5.02  | 5.77  |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
|                |       |       |       |       |       |       |       |       |       |       | HAZ   |
| Urban Forest   |       |       |       |       |       |       |       |       |       |       |       |
|                | 13.66 | 0.27  | 2.25  | 1.56  | -2.04 | -1.74 | -0.45 | 0.01  | -0.36 | -1.05 | 0.13  |
|                | 12.51 | 0.35  | 1.99  | 2.64  | -0.70 | -0.52 | 1.11  | 1.81  | 1.17  | 0.75  | 2.47  |
|                | 12.27 | -0.49 | 1.58  | 2.10  | -1.34 | -1.44 | -0.10 | 0.51  | 0.20  | 0.02  | 1.41  |
|                | 12.09 | 1.28  | 2.60  | 2.73  | -0.88 | 0.10  | 1.94  | 3.63  | 3.57  | 3.14  | 5.06  |
|                | 11.96 | 3.31  | 3.82  | 4.68  | 1.91  | 1.79  | 2.59  | 4.54  | 5.08  | 4.67  | 6.35  |
| ln(y)          | 11.81 | 4.70  | 4.10  | 4.36  | 2.57  | 2.83  | 3.02  | 5.17  | 5.69  | 5.28  | 6.52  |
|                | 11.67 | 3.85  | 2.45  | 4.22  | 2.58  | 4.02  | 4.08  | 5.65  | 6.16  | 5.66  | 7.30  |
|                | 11.51 | 4.60  | 2.68  | 4.10  | 2.42  | 3.98  | 4.33  | 5.58  | 5.84  | 5.52  | 6.44  |
|                | 11.31 | 1.22  | 0.15  | 2.40  | 0.78  | 1.06  | -0.23 | 1.36  | 1.11  | 1.22  | 2.38  |
|                | 11.07 | 4.18  | -0.56 | 1.70  | -0.82 | 1.41  | -0.11 | 2.69  | 2.13  | 1.63  | 2.19  |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
|                |       |       |       |       |       |       |       |       |       |       | HAZ   |
| Urban Savannah |       |       |       |       |       |       |       |       |       |       |       |
|                | 13.66 | -1.67 | -0.91 | 2.56  | 0.12  | 2.88  | 4.45  | 4.76  | 2.85  | 2.34  | 0.00  |
|                | 12.51 | -0.31 | -0.29 | 3.48  | 1.92  | 4.06  | 5.07  | 5.95  | 4.38  | 3.40  | 1.29  |
|                | 12.27 | -1.15 | -1.05 | 1.80  | 0.66  | 2.62  | 3.97  | 5.71  | 4.25  | 3.46  | 1.12  |
|                | 12.09 | -1.44 | -0.60 | 1.83  | -0.23 | 1.53  | 4.52  | 6.20  | 4.58  | 3.16  | 0.37  |
|                | 11.96 | -1.74 | -1.42 | 1.43  | -0.30 | 0.47  | 2.21  | 3.91  | 3.25  | 1.77  | -1.67 |
| ln(y)          | 11.81 | -0.85 | -0.01 | 4.13  | 2.61  | 4.22  | 6.47  | 7.59  | 6.72  | 5.10  | 1.57  |
|                | 11.67 | 5.35  | 4.89  | 9.77  | 7.64  | 7.85  | 9.57  | 10.68 | 10.80 | 8.89  | 5.77  |
|                | 11.51 | 3.62  | 4.86  | 8.75  | 9.97  | 10.69 | 11.39 | 10.88 | 10.76 | 11.16 | 7.49  |
|                | 11.31 | 0.20  | 0.63  | 4.03  | 4.64  | 4.37  | 3.64  | 2.60  | 1.56  | 1.63  | -0.63 |
|                | 11.07 | 1.13  | 3.31  | 5.45  | 5.83  | 5.02  | 5.35  | 3.75  | 0.91  | 1.46  | 3.03  |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
|                |       |       |       |       |       |       |       |       |       |       | HAZ   |

**Table A. 3 -  $\Pi^{1,1}$  Dominance Tests for Rural Forest vs. Urban Areas in Ghana**

| Urban Coast    |       |       |       |       |       |       |       |       |       |       |       |
|----------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|                | 13.66 | 11.26 | 14.92 | 14.56 | 12.12 | 9.99  | 10.29 | 7.69  | 4.12  | 1.59  | 0.13  |
|                | 12.51 | 10.49 | 14.74 | 14.81 | 12.72 | 10.84 | 11.54 | 9.80  | 6.70  | 5.09  | 4.52  |
|                | 12.27 | 9.99  | 14.59 | 14.74 | 13.18 | 12.47 | 13.06 | 11.47 | 9.46  | 8.06  | 7.66  |
|                | 12.09 | 9.59  | 15.79 | 16.69 | 15.07 | 13.98 | 15.05 | 13.25 | 12.23 | 11.49 | 11.25 |
|                | 11.96 | 10.40 | 15.86 | 16.31 | 15.00 | 14.17 | 15.53 | 13.95 | 13.40 | 12.54 | 12.05 |
| ln(y)          | 11.81 | 11.59 | 15.74 | 16.73 | 14.65 | 13.62 | 14.90 | 13.58 | 13.39 | 12.10 | 11.29 |
|                | 11.67 | 9.39  | 12.63 | 14.27 | 12.45 | 12.22 | 12.80 | 12.14 | 11.56 | 10.92 | 10.29 |
|                | 11.51 | 7.63  | 10.97 | 12.76 | 11.42 | 10.80 | 11.82 | 11.45 | 11.03 | 10.15 | 9.78  |
|                | 11.31 | 5.90  | 7.71  | 9.68  | 8.87  | 8.17  | 8.78  | 9.03  | 8.86  | 8.19  | 8.33  |
|                | 11.07 | 4.16  | 5.62  | 6.46  | 6.63  | 6.44  | 6.49  | 7.51  | 7.11  | 6.88  | 7.41  |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
| HAZ            |       |       |       |       |       |       |       |       |       |       |       |
| Urban Forest   |       |       |       |       |       |       |       |       |       |       |       |
|                | 13.66 | 5.17  | 9.04  | 7.74  | 3.93  | 3.23  | 4.15  | 2.64  | 1.67  | 1.38  | 0.08  |
|                | 12.51 | 5.78  | 9.06  | 8.98  | 4.93  | 4.08  | 5.27  | 4.09  | 2.90  | 3.05  | 2.43  |
|                | 12.27 | 4.42  | 7.48  | 7.75  | 3.74  | 2.36  | 3.04  | 1.77  | 0.99  | 1.18  | 0.40  |
|                | 12.09 | 5.61  | 8.98  | 8.72  | 4.69  | 4.06  | 5.25  | 4.43  | 4.13  | 4.27  | 4.02  |
|                | 11.96 | 7.30  | 9.67  | 9.71  | 6.57  | 5.29  | 6.26  | 5.31  | 5.46  | 5.79  | 5.26  |
| ln(y)          | 11.81 | 8.34  | 9.82  | 9.81  | 7.84  | 6.37  | 6.65  | 6.59  | 6.47  | 6.44  | 5.82  |
|                | 11.67 | 6.12  | 6.69  | 8.39  | 5.83  | 6.05  | 6.12  | 5.47  | 5.06  | 4.79  | 4.48  |
|                | 11.51 | 5.29  | 4.57  | 6.35  | 3.88  | 3.72  | 4.24  | 3.91  | 4.00  | 3.56  | 3.07  |
|                | 11.31 | 3.45  | 2.26  | 4.81  | 2.30  | 1.41  | 1.17  | 1.67  | 1.67  | 1.46  | 1.69  |
|                | 11.07 | 4.71  | 2.19  | 3.79  | 1.75  | 3.32  | 2.58  | 4.11  | 3.95  | 3.52  | 3.85  |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
| HAZ            |       |       |       |       |       |       |       |       |       |       |       |
| Urban Savannah |       |       |       |       |       |       |       |       |       |       |       |
|                | 13.66 | 3.22  | 5.85  | 8.75  | 6.11  | 7.90  | 9.13  | 7.43  | 4.89  | 4.78  | -0.05 |
|                | 12.51 | 5.13  | 6.75  | 9.84  | 7.59  | 8.74  | 9.31  | 8.26  | 6.13  | 5.72  | 1.26  |
|                | 12.27 | 3.76  | 4.83  | 7.45  | 5.75  | 6.44  | 7.14  | 7.00  | 5.04  | 4.63  | 0.11  |
|                | 12.09 | 2.91  | 5.77  | 7.81  | 5.34  | 5.50  | 7.87  | 7.02  | 5.14  | 4.29  | -0.65 |
|                | 11.96 | 2.31  | 4.42  | 6.43  | 4.34  | 3.96  | 5.87  | 4.69  | 3.62  | 2.88  | -2.74 |
| ln(y)          | 11.81 | 2.89  | 5.72  | 9.59  | 7.88  | 7.78  | 10.15 | 9.03  | 7.50  | 6.26  | 0.87  |
|                | 11.67 | 7.58  | 9.11  | 13.91 | 10.92 | 9.90  | 11.65 | 10.49 | 9.68  | 8.01  | 2.96  |
|                | 11.51 | 4.31  | 6.73  | 10.96 | 11.42 | 10.43 | 11.30 | 9.19  | 8.90  | 9.15  | 4.10  |
|                | 11.31 | 2.45  | 2.74  | 6.42  | 6.14  | 4.73  | 5.04  | 2.92  | 2.12  | 1.87  | -1.32 |
|                | 11.07 | 1.73  | 5.91  | 7.40  | 8.18  | 6.87  | 7.92  | 5.17  | 2.73  | 3.35  | 4.68  |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
| HAZ            |       |       |       |       |       |       |       |       |       |       |       |

**Table A. 4 -  $\Pi^{1,1}$  Dominance Tests for Rural Savannah vs. Urban Areas in Ghana**

| Urban Coast    |       |       |       |       |       |       |       |       |       |       |       |
|----------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|                | 13.66 | 10.53 | 13.44 | 12.76 | 10.38 | 8.66  | 8.05  | 6.87  | 3.48  | 1.46  | 0.17  |
|                | 12.51 | 10.35 | 13.91 | 13.99 | 12.48 | 11.01 | 11.25 | 11.05 | 8.29  | 6.94  | 6.48  |
|                | 12.27 | 10.65 | 14.26 | 14.79 | 13.46 | 13.31 | 13.91 | 13.68 | 12.03 | 11.03 | 10.67 |
|                | 12.09 | 10.36 | 15.62 | 16.82 | 15.22 | 15.03 | 15.58 | 15.31 | 14.84 | 14.75 | 14.71 |
|                | 11.96 | 10.99 | 15.35 | 15.99 | 14.67 | 14.95 | 16.05 | 15.87 | 15.97 | 15.48 | 15.53 |
| ln(y)          | 11.81 | 11.70 | 16.13 | 17.25 | 15.09 | 15.85 | 17.36 | 17.07 | 17.69 | 16.75 | 16.49 |
|                | 11.67 | 10.68 | 13.94 | 15.48 | 14.47 | 15.79 | 16.63 | 17.30 | 17.34 | 17.44 | 17.49 |
|                | 11.51 | 10.43 | 13.91 | 15.65 | 14.70 | 15.21 | 17.09 | 18.35 | 18.69 | 18.75 | 18.88 |
|                | 11.31 | 8.57  | 11.74 | 13.29 | 13.42 | 13.59 | 14.85 | 15.17 | 15.73 | 15.90 | 15.98 |
|                | 11.07 | 7.74  | 8.87  | 10.68 | 11.31 | 11.66 | 12.49 | 13.06 | 12.45 | 13.10 | 13.27 |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
|                |       |       |       |       |       |       |       |       |       |       | HAZ   |
| Urban Forest   |       |       |       |       |       |       |       |       |       |       |       |
|                | 13.66 | 4.42  | 7.59  | 6.01  | 2.26  | 1.94  | 1.98  | 1.83  | 1.03  | 1.25  | 0.13  |
|                | 12.51 | 5.64  | 8.25  | 8.20  | 4.70  | 4.24  | 5.00  | 5.29  | 4.46  | 4.89  | 4.38  |
|                | 12.27 | 5.10  | 7.15  | 7.79  | 4.01  | 3.15  | 3.84  | 3.85  | 3.44  | 4.05  | 3.31  |
|                | 12.09 | 6.39  | 8.81  | 8.85  | 4.82  | 5.05  | 5.75  | 6.35  | 6.58  | 7.34  | 7.27  |
|                | 11.96 | 7.91  | 9.16  | 9.39  | 6.25  | 6.02  | 6.74  | 7.10  | 7.85  | 8.56  | 8.53  |
| ln(y)          | 11.81 | 8.45  | 10.22 | 10.32 | 8.26  | 8.50  | 8.95  | 9.88  | 10.52 | 10.86 | 10.77 |
|                | 11.67 | 7.48  | 8.03  | 9.60  | 7.81  | 9.52  | 9.79  | 10.39 | 10.57 | 11.01 | 11.35 |
|                | 11.51 | 8.27  | 7.67  | 9.30  | 7.16  | 8.08  | 9.37  | 10.58 | 11.37 | 11.81 | 11.76 |
|                | 11.31 | 6.29  | 6.53  | 8.56  | 6.96  | 6.89  | 7.25  | 7.78  | 8.44  | 9.04  | 9.17  |
|                | 11.07 | 8.19  | 5.66  | 8.22  | 6.73  | 8.71  | 8.76  | 9.81  | 9.39  | 9.82  | 9.78  |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
|                |       |       |       |       |       |       |       |       |       |       | HAZ   |
| Urban Savannah |       |       |       |       |       |       |       |       |       |       |       |
|                | 13.66 | 2.47  | 4.41  | 7.02  | 4.43  | 6.59  | 6.91  | 6.61  | 4.25  | 4.65  | 0.00  |
|                | 12.51 | 4.98  | 5.95  | 9.05  | 7.35  | 8.91  | 9.03  | 9.49  | 7.71  | 7.58  | 3.20  |
|                | 12.27 | 4.44  | 4.51  | 7.49  | 6.02  | 7.25  | 7.96  | 9.13  | 7.53  | 7.54  | 3.01  |
|                | 12.09 | 3.70  | 5.60  | 7.94  | 5.48  | 6.49  | 8.37  | 8.96  | 7.60  | 7.36  | 2.55  |
|                | 11.96 | 2.93  | 3.91  | 6.11  | 4.02  | 4.69  | 6.36  | 6.47  | 6.00  | 5.61  | 0.47  |
| ln(y)          | 11.81 | 3.01  | 6.12  | 10.09 | 8.30  | 9.92  | 12.51 | 12.38 | 11.57 | 10.67 | 5.70  |
|                | 11.67 | 8.91  | 10.44 | 15.13 | 12.92 | 13.43 | 15.45 | 15.57 | 15.36 | 14.37 | 9.77  |
|                | 11.51 | 7.34  | 9.79  | 13.88 | 14.70 | 14.84 | 16.55 | 16.01 | 16.46 | 17.68 | 12.84 |
|                | 11.31 | 5.33  | 6.99  | 10.14 | 10.76 | 10.19 | 11.12 | 9.04  | 8.89  | 9.46  | 6.12  |
|                | 11.07 | 5.65  | 9.13  | 11.52 | 12.69 | 12.05 | 13.81 | 10.83 | 8.19  | 9.66  | 10.60 |
|                | 0.00  | -3.09 | -2.41 | -1.93 | -1.56 | -1.20 | -0.84 | -0.50 | -0.07 | 0.60  | 5.05  |
|                |       |       |       |       |       |       |       |       |       |       | HAZ   |

**Table A. 5 -  $\Pi^{1,1}$  Dominance Tests for Rural and Urban Areas in Madagascar**

|       |       |       |       |       |       |        |        |        |        |        |        |
|-------|-------|-------|-------|-------|-------|--------|--------|--------|--------|--------|--------|
|       | 16.51 | 3.259 | 2.949 | 3.145 | 3.257 | 3.913  | 4.167  | 2.588  | 1.153  | 0.292  | -0.079 |
|       | 13.19 | 3.687 | 3.171 | 4.066 | 4.623 | 5.541  | 6.504  | 5.412  | 4.839  | 4.627  | 4.821  |
|       | 12.84 | 3.484 | 4.453 | 5.105 | 6.525 | 7.979  | 9.151  | 8.523  | 8.430  | 8.343  | 8.698  |
|       | 12.60 | 5.292 | 5.470 | 6.317 | 8.224 | 10.020 | 11.630 | 10.930 | 10.820 | 11.090 | 11.360 |
|       | 12.44 | 5.221 | 5.663 | 6.294 | 8.150 | 10.350 | 12.500 | 12.310 | 12.310 | 12.970 | 12.750 |
| ln(y) | 12.29 | 5.073 | 6.592 | 6.468 | 8.577 | 10.300 | 12.000 | 11.690 | 11.660 | 12.380 | 12.320 |
|       | 12.16 | 3.876 | 5.762 | 5.602 | 7.566 | 8.466  | 10.410 | 10.650 | 10.490 | 11.470 | 11.240 |
|       | 12.00 | 3.563 | 6.439 | 5.626 | 7.593 | 9.052  | 10.530 | 10.830 | 11.170 | 12.000 | 12.540 |
|       | 11.82 | 3.466 | 5.865 | 4.413 | 5.684 | 6.488  | 7.695  | 7.811  | 8.012  | 8.739  | 8.920  |
|       | 11.48 | 2.052 | 3.102 | 1.728 | 2.724 | 3.284  | 4.498  | 5.387  | 5.529  | 6.426  | 7.551  |
|       | 0.000 | -4.01 | -3.33 | -2.84 | -2.39 | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|       |       | HAZ   |       |       |       |        |        |        |        |        |        |

**Table A. 6 -  $\Pi^{1,1}$  Dominance Tests for Rural Antananarivo vs. Urban Areas in Madagascar**

| Urban Antananarivo           |       |        |        |        |        |        |        |        |        |        |        |
|------------------------------|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|                              | 16.51 | 3.154  | 6.363  | 7.837  | 9.405  | 10.940 | 10.290 | 6.959  | 3.581  | 1.588  | 0.000  |
|                              | 13.19 | 4.785  | 7.602  | 9.615  | 11.940 | 14.720 | 14.680 | 11.490 | 8.881  | 7.933  | 7.248  |
|                              | 12.84 | 6.338  | 11.820 | 13.210 | 16.750 | 19.820 | 20.440 | 17.610 | 15.640 | 14.800 | 14.270 |
|                              | 12.60 | 7.723  | 12.460 | 12.600 | 16.500 | 18.310 | 19.590 | 17.260 | 15.950 | 15.170 | 14.490 |
|                              | 12.44 | 8.387  | 13.230 | 13.630 | 17.130 | 18.910 | 21.750 | 19.510 | 18.240 | 17.970 | 16.600 |
| ln(y)                        | 12.29 | 8.149  | 13.590 | 13.200 | 16.710 | 17.630 | 19.610 | 17.400 | 15.820 | 15.300 | 14.300 |
|                              | 12.16 | 6.834  | 11.180 | 11.470 | 14.410 | 13.890 | 15.140 | 13.520 | 11.380 | 10.760 | 10.230 |
|                              | 12.00 | 5.162  | 8.562  | 8.396  | 10.540 | 11.060 | 11.890 | 10.650 | 9.516  | 8.793  | 9.012  |
|                              | 11.82 | 5.113  | 7.359  | 7.405  | 9.297  | 8.843  | 9.364  | 8.167  | 6.638  | 6.265  | 5.949  |
|                              | 11.48 | 3.553  | 3.404  | 3.627  | 4.172  | 3.763  | 4.526  | 4.146  | 3.631  | 3.527  | 3.760  |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
| HAZ                          |       |        |        |        |        |        |        |        |        |        |        |
| Urban Fianarantsoa/Toamasina |       |        |        |        |        |        |        |        |        |        |        |
|                              | 16.51 | 2.106  | 2.428  | 6.446  | 6.273  | 6.262  | 9.066  | 8.314  | 6.290  | 3.529  | 0.000  |
|                              | 13.19 | 1.409  | 1.984  | 6.472  | 7.246  | 7.127  | 10.540 | 9.651  | 8.686  | 6.570  | 3.550  |
|                              | 12.84 | 2.370  | 3.034  | 7.464  | 8.607  | 9.410  | 13.310 | 12.180 | 11.960 | 10.630 | 7.689  |
|                              | 12.60 | 4.246  | 5.497  | 9.127  | 10.620 | 11.130 | 15.040 | 14.640 | 15.170 | 13.980 | 10.900 |
|                              | 12.44 | 4.176  | 5.669  | 9.549  | 10.670 | 12.420 | 16.090 | 15.220 | 16.000 | 14.260 | 10.490 |
| ln(y)                        | 12.29 | 5.671  | 6.274  | 8.983  | 9.736  | 10.850 | 13.800 | 13.320 | 13.890 | 11.740 | 8.487  |
|                              | 12.16 | 4.867  | 5.794  | 8.998  | 10.220 | 10.740 | 13.570 | 13.090 | 14.660 | 12.590 | 9.205  |
|                              | 12.00 | 2.845  | 6.403  | 7.495  | 9.909  | 11.090 | 13.720 | 13.610 | 14.800 | 12.430 | 10.010 |
|                              | 11.82 | 4.489  | 9.217  | 8.933  | 9.535  | 10.140 | 11.880 | 11.480 | 11.910 | 9.359  | 5.946  |
|                              | 11.48 | 3.770  | 5.577  | 6.521  | 5.935  | 6.268  | 7.321  | 8.667  | 8.323  | 8.536  | 8.763  |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
| HAZ                          |       |        |        |        |        |        |        |        |        |        |        |
| Urban Mahajanga/Antsiranana  |       |        |        |        |        |        |        |        |        |        |        |
|                              | 16.51 | 14.210 | 15.050 | 18.070 | 17.130 | 15.210 | 13.230 | 7.546  | 6.791  | 3.026  | 0.000  |
|                              | 13.19 | 14.410 | 15.230 | 19.150 | 19.060 | 17.920 | 17.680 | 12.640 | 12.730 | 8.742  | 6.758  |
|                              | 12.84 | 14.410 | 16.010 | 19.510 | 21.280 | 21.330 | 20.620 | 16.490 | 16.990 | 12.540 | 11.350 |
|                              | 12.60 | 14.280 | 15.460 | 19.170 | 23.510 | 27.120 | 26.570 | 20.930 | 21.420 | 16.800 | 16.350 |
|                              | 12.44 | 13.640 | 18.010 | 21.090 | 26.460 | 30.730 | 29.350 | 25.240 | 25.690 | 22.470 | 21.840 |
| ln(y)                        | 12.29 | 12.450 | 16.700 | 19.140 | 24.790 | 27.970 | 26.600 | 22.930 | 23.910 | 20.990 | 21.290 |
|                              | 12.16 | 11.920 | 14.750 | 15.990 | 20.540 | 22.200 | 23.240 | 20.620 | 20.940 | 20.140 | 20.480 |
|                              | 12.00 | 9.061  | 13.170 | 13.040 | 16.540 | 18.000 | 19.150 | 17.620 | 17.610 | 16.790 | 16.880 |
|                              | 11.82 | 8.900  | 12.250 | 11.830 | 13.930 | 14.550 | 15.060 | 13.740 | 13.330 | 12.110 | 11.350 |
|                              | 11.48 | 5.364  | 7.045  | 4.937  | 4.659  | 4.856  | 5.257  | 6.629  | 5.386  | 4.883  | 5.116  |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
| HAZ                          |       |        |        |        |        |        |        |        |        |        |        |

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Urban Toliara

|       |       |        |        |        |        |        |        |        |        |        |        |
|-------|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|       | 16.51 | -5.614 | -9.693 | -9.164 | -3.390 | -0.148 | 2.859  | 1.683  | 2.302  | 2.324  | 0.000  |
|       | 13.19 | -4.391 | -9.085 | -7.892 | -2.117 | 0.818  | 4.131  | 2.215  | 2.989  | 3.255  | 1.149  |
|       | 12.84 | -4.391 | -6.766 | -6.419 | -0.958 | 2.653  | 6.021  | 4.326  | 5.505  | 6.060  | 4.405  |
|       | 12.60 | 3.182  | -1.986 | 0.484  | 6.088  | 8.402  | 11.940 | 10.980 | 11.880 | 11.690 | 9.382  |
|       | 12.44 | 7.361  | -1.111 | 1.040  | 6.074  | 8.391  | 11.780 | 10.710 | 11.360 | 11.200 | 8.572  |
| ln(y) | 12.29 | 6.803  | 3.115  | 4.168  | 9.193  | 11.360 | 13.850 | 12.550 | 12.590 | 13.030 | 10.070 |
|       | 12.16 | 4.859  | 4.084  | 3.795  | 7.917  | 8.773  | 10.870 | 10.420 | 9.881  | 10.220 | 6.841  |
|       | 12.00 | 9.356  | 9.943  | 9.561  | 12.940 | 13.900 | 15.850 | 15.150 | 14.560 | 14.360 | 12.650 |
|       | 11.82 | 10.600 | 9.165  | 9.140  | 11.090 | 11.970 | 13.700 | 12.150 | 10.560 | 10.530 | 9.297  |
|       | 11.48 | 7.546  | 3.865  | 3.070  | 3.572  | 4.648  | 5.718  | 5.467  | 4.719  | 4.135  | 3.833  |
|       | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|       |       |        |        |        |        | HAZ    |        |        |        |        |        |

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**Table A. 7 -  $\Pi^{1,1}$  Dominance Tests for Rural Fianarantsoa/Toamasina vs. Urban Areas in Madagascar**

| Urban Antananarivo           |       |        |        |        |        |        |        |        |        |        |        |
|------------------------------|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|                              | 16.51 | 7.198  | 10.440 | 8.607  | 6.840  | 7.968  | 6.849  | 4.194  | 0.252  | -0.352 | -0.045 |
|                              | 13.19 | 8.944  | 11.720 | 10.480 | 9.473  | 11.520 | 10.910 | 9.079  | 6.192  | 6.864  | 7.931  |
|                              | 12.84 | 9.165  | 14.770 | 13.320 | 13.670 | 15.760 | 15.780 | 14.330 | 11.660 | 12.890 | 13.820 |
|                              | 12.60 | 9.872  | 14.840 | 12.820 | 13.200 | 14.670 | 15.790 | 14.630 | 12.360 | 14.250 | 14.990 |
|                              | 12.44 | 8.096  | 13.740 | 11.580 | 11.820 | 13.310 | 16.220 | 15.560 | 13.500 | 15.920 | 16.400 |
| ln(y)                        | 12.29 | 7.009  | 13.270 | 10.620 | 11.510 | 12.200 | 14.850 | 13.930 | 11.860 | 13.830 | 14.570 |
|                              | 12.16 | 4.814  | 10.490 | 8.589  | 9.168  | 9.433  | 11.390 | 10.550 | 7.979  | 9.182  | 10.190 |
|                              | 12.00 | 3.847  | 7.867  | 5.833  | 6.076  | 7.441  | 8.533  | 7.917  | 6.756  | 7.945  | 9.620  |
|                              | 11.82 | 1.936  | 5.089  | 2.706  | 2.738  | 2.943  | 4.488  | 4.422  | 3.745  | 5.232  | 7.110  |
|                              | 11.48 | 0.117  | 2.651  | 0.830  | 0.851  | 0.635  | 2.827  | 2.439  | 2.744  | 3.952  | 5.921  |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
| HAZ                          |       |        |        |        |        |        |        |        |        |        |        |
| Urban Fianarantsoa/Toamasina |       |        |        |        |        |        |        |        |        |        |        |
|                              | 16.51 | 6.155  | 6.463  | 7.211  | 3.745  | 3.368  | 5.647  | 5.530  | 2.935  | 1.584  | -0.045 |
|                              | 13.19 | 5.592  | 6.048  | 7.329  | 4.839  | 4.086  | 6.899  | 7.270  | 6.000  | 5.510  | 4.220  |
|                              | 12.84 | 5.227  | 5.928  | 7.574  | 5.700  | 5.696  | 8.977  | 9.068  | 8.109  | 8.796  | 7.260  |
|                              | 12.60 | 6.428  | 7.847  | 9.345  | 7.449  | 7.698  | 11.410 | 12.080 | 11.610 | 13.070 | 11.380 |
|                              | 12.44 | 3.878  | 6.176  | 7.535  | 5.560  | 7.091  | 10.870 | 11.440 | 11.360 | 12.290 | 10.300 |
| ln(y)                        | 12.29 | 4.507  | 5.954  | 6.426  | 4.703  | 5.634  | 9.267  | 9.967  | 10.010 | 10.320 | 8.745  |
|                              | 12.16 | 2.812  | 5.090  | 6.120  | 5.038  | 6.334  | 9.848  | 10.120 | 11.190 | 11.000 | 9.158  |
|                              | 12.00 | 1.501  | 5.697  | 4.928  | 5.447  | 7.471  | 10.340 | 10.840 | 11.980 | 11.570 | 10.620 |
|                              | 11.82 | 1.282  | 7.015  | 4.276  | 2.980  | 4.257  | 7.019  | 7.733  | 9.012  | 8.322  | 7.107  |
|                              | 11.48 | 0.350  | 4.867  | 3.824  | 2.661  | 3.191  | 5.660  | 7.013  | 7.461  | 8.949  | 10.860 |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
| HAZ                          |       |        |        |        |        |        |        |        |        |        |        |
| Urban Mahajanga/Antsiranana  |       |        |        |        |        |        |        |        |        |        |        |
|                              | 16.51 | 17.970 | 19.250 | 18.890 | 14.410 | 12.140 | 9.703  | 4.774  | 3.429  | 1.083  | -0.045 |
|                              | 13.19 | 18.240 | 19.440 | 20.090 | 16.430 | 14.620 | 13.790 | 10.200 | 9.965  | 7.668  | 7.438  |
|                              | 12.84 | 17.010 | 18.990 | 19.630 | 18.070 | 17.200 | 15.950 | 13.240 | 12.940 | 10.670 | 10.910 |
|                              | 12.60 | 16.270 | 17.860 | 19.400 | 19.980 | 23.080 | 22.410 | 18.190 | 17.590 | 15.870 | 16.860 |
|                              | 12.44 | 13.370 | 18.520 | 18.970 | 20.720 | 24.380 | 23.270 | 21.010 | 20.480 | 20.290 | 21.620 |
| ln(y)                        | 12.29 | 11.390 | 16.380 | 16.520 | 19.330 | 22.030 | 21.490 | 19.250 | 19.600 | 19.420 | 21.590 |
|                              | 12.16 | 10.120 | 14.080 | 13.110 | 15.200 | 17.550 | 19.270 | 17.490 | 17.290 | 18.440 | 20.430 |
|                              | 12.00 | 7.870  | 12.520 | 10.520 | 12.100 | 14.360 | 15.720 | 14.810 | 14.750 | 15.910 | 17.520 |
|                              | 11.82 | 6.126  | 10.230 | 7.312  | 7.536  | 8.781  | 10.250 | 10.000 | 10.430 | 11.070 | 12.520 |
|                              | 11.48 | 2.151  | 6.384  | 2.172  | 1.348  | 1.744  | 3.564  | 4.943  | 4.505  | 5.307  | 7.266  |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
| HAZ                          |       |        |        |        |        |        |        |        |        |        |        |

Urban Toliara

|       |       |        |        |        |        |        |        |        |        |        |        |
|-------|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|       | 16.51 | -1.560 | -5.611 | -8.389 | -5.916 | -3.019 | -0.488 | -1.046 | -1.023 | 0.383  | -0.045 |
|       | 13.19 | -0.204 | -4.982 | -7.031 | -4.503 | -2.188 | 0.590  | -0.098 | 0.360  | 2.208  | 1.815  |
|       | 12.84 | -1.530 | -3.863 | -6.309 | -3.820 | -0.983 | 1.869  | 1.339  | 1.787  | 4.278  | 3.983  |
|       | 12.60 | 5.369  | 0.348  | 0.696  | 2.984  | 5.022  | 8.410  | 8.506  | 8.424  | 10.800 | 9.858  |
|       | 12.44 | 7.067  | -0.606 | -0.941 | 1.047  | 3.173  | 6.728  | 7.064  | 6.894  | 9.284  | 8.383  |
| ln(y) | 12.29 | 5.648  | 2.795  | 1.634  | 4.169  | 6.124  | 9.312  | 9.217  | 8.742  | 11.590 | 10.330 |
|       | 12.16 | 2.804  | 3.380  | 0.930  | 2.767  | 4.399  | 7.199  | 7.501  | 6.510  | 8.654  | 6.794  |
|       | 12.00 | 8.180  | 9.257  | 7.006  | 8.478  | 10.260 | 12.450 | 12.360 | 11.740 | 13.490 | 13.270 |
|       | 11.82 | 8.183  | 6.961  | 4.490  | 4.580  | 6.119  | 8.863  | 8.407  | 7.657  | 9.489  | 10.470 |
|       | 11.48 | 5.018  | 3.118  | 0.265  | 0.242  | 1.533  | 4.031  | 3.769  | 3.835  | 4.559  | 5.993  |
|       | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|       |       |        |        |        |        |        |        |        |        |        | HAZ    |

**Table A. 8 -  $\Pi^{1,1}$  Dominance Tests for Rural Mahajanga/Antsiranana vs. Urban Areas in Madagascar**

| Urban Antananarivo           |       |         |         |         |         |         |        |        |        |        |        |
|------------------------------|-------|---------|---------|---------|---------|---------|--------|--------|--------|--------|--------|
|                              | 16.51 | -3.434  | -3.306  | -6.104  | -5.625  | -4.052  | -4.033 | -4.128 | -5.822 | -4.624 | -0.143 |
|                              | 13.19 | -2.647  | -2.835  | -4.799  | -4.747  | -2.894  | -2.708 | -2.413 | -3.765 | -1.785 | 3.091  |
|                              | 12.84 | -3.947  | -1.045  | -3.290  | -2.245  | -0.286  | -0.096 | 0.959  | 0.514  | 1.711  | 6.764  |
|                              | 12.60 | -6.668  | -4.166  | -7.532  | -6.180  | -4.204  | -3.623 | -3.435 | -4.298 | -2.226 | 2.354  |
|                              | 12.44 | -7.125  | -4.802  | -8.739  | -8.156  | -6.047  | -3.577 | -2.983 | -3.886 | -1.888 | 1.362  |
| ln(y)                        | 12.29 | -6.127  | -2.246  | -7.511  | -6.629  | -5.424  | -3.854 | -3.141 | -3.836 | -1.357 | 1.547  |
|                              | 12.16 | -6.937  | -3.922  | -7.983  | -6.639  | -8.157  | -6.329 | -4.620 | -5.842 | -3.338 | -1.309 |
|                              | 12.00 | -6.713  | -3.300  | -7.326  | -6.481  | -6.738  | -5.521 | -4.281 | -4.165 | -2.103 | 0.381  |
|                              | 11.82 | -5.356  | -6.554  | -9.495  | -6.904  | -8.085  | -7.011 | -6.205 | -6.107 | -4.656 | -2.258 |
|                              | 11.48 | -3.138  | -3.753  | -6.962  | -5.021  | -6.444  | -5.215 | -5.080 | -4.279 | -2.868 | -0.913 |
|                              | 0.000 | -4.01   | -3.33   | -2.84   | -2.39   | -1.98   | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|                              |       | HAZ     |         |         |         |         |        |        |        |        |        |
| Urban Fianarantsoa/Toamasina |       |         |         |         |         |         |        |        |        |        |        |
|                              | 16.51 | -4.477  | -7.239  | -7.489  | -8.740  | -8.663  | -5.226 | -2.798 | -3.119 | -2.677 | -0.143 |
|                              | 13.19 | -6.003  | -8.447  | -7.912  | -9.370  | -10.270 | -6.635 | -4.182 | -3.955 | -3.121 | -0.563 |
|                              | 12.84 | -7.849  | -9.798  | -8.923  | -10.070 | -10.060 | -6.569 | -4.042 | -2.901 | -2.195 | 0.468  |
|                              | 12.60 | -9.933  | -11.040 | -10.940 | -11.850 | -11.010 | -7.779 | -5.841 | -5.012 | -3.327 | -1.022 |
|                              | 12.44 | -10.940 | -12.200 | -12.710 | -14.400 | -12.190 | -8.691 | -6.890 | -5.929 | -5.280 | -4.349 |
| ln(y)                        | 12.29 | -8.442  | -9.563  | -11.610 | -13.380 | -11.930 | -9.274 | -6.966 | -5.637 | -4.710 | -4.011 |
|                              | 12.16 | -8.681  | -9.238  | -10.380 | -10.720 | -11.220 | -7.839 | -5.033 | -2.699 | -1.574 | -2.308 |
|                              | 12.00 | -8.645  | -5.481  | -8.202  | -7.102  | -6.709  | -3.724 | -1.384 | 0.997  | 1.457  | 1.362  |
|                              | 11.82 | -5.908  | -4.744  | -8.107  | -6.670  | -6.814  | -4.507 | -2.902 | -0.841 | -1.575 | -2.261 |
|                              | 11.48 | -2.927  | -1.513  | -4.275  | -3.270  | -4.005  | -2.396 | -0.456 | 0.514  | 2.263  | 4.203  |
|                              | 0.000 | -4.01   | -3.33   | -2.84   | -2.39   | -1.98   | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|                              |       | HAZ     |         |         |         |         |        |        |        |        |        |
| Urban Mahajanga/Antsiranana  |       |         |         |         |         |         |        |        |        |        |        |
|                              | 16.51 | 8.146   | 5.343   | 3.746   | 1.689   | -0.024  | -1.246 | -3.550 | -2.625 | -3.179 | -0.143 |
|                              | 13.19 | 7.689   | 4.798   | 4.353   | 1.882   | 0.036   | 0.015  | -1.327 | -0.086 | -0.999 | 2.608  |
|                              | 12.84 | 4.997   | 3.211   | 2.738   | 1.883   | 1.041   | 0.060  | -0.051 | 1.729  | -0.387 | 3.998  |
|                              | 12.60 | 0.644   | -1.109  | -1.199  | 0.219   | 3.480   | 2.308  | -0.187 | 0.533  | -0.742 | 4.052  |
|                              | 12.44 | -1.392  | 0.310   | -1.472  | 0.433   | 4.310   | 2.820  | 1.950  | 2.485  | 2.024  | 5.979  |
| ln(y)                        | 12.29 | -1.392  | 1.197   | -1.597  | 1.090   | 4.079   | 2.364  | 1.814  | 3.376  | 3.782  | 7.901  |
|                              | 12.16 | -1.389  | 0.024   | -3.463  | -0.589  | -0.127  | 1.329  | 2.069  | 3.143  | 5.481  | 8.325  |
|                              | 12.00 | -2.881  | 1.931   | -2.609  | -0.378  | 0.256   | 1.685  | 2.549  | 3.721  | 5.677  | 8.027  |
|                              | 11.82 | -1.200  | -1.045  | -5.280  | -2.126  | -2.281  | -1.212 | -0.597 | 0.593  | 1.183  | 3.129  |
|                              | 11.48 | -1.200  | 0.309   | -5.786  | -4.546  | -5.398  | -4.496 | -2.592 | -2.522 | -1.505 | 0.455  |
|                              | 0.000 | -4.01   | -3.33   | -2.84   | -2.39   | -1.98   | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|                              |       | HAZ     |         |         |         |         |        |        |        |        |        |

Urban Toliara

|       |       |         |         |         |         |         |         |         |         |        |        |
|-------|-------|---------|---------|---------|---------|---------|---------|---------|---------|--------|--------|
|       | 16.51 | -12.130 | -19.800 | -24.320 | -19.060 | -15.400 | -11.510 | -9.463  | -7.120  | -3.883 | -0.143 |
|       | 13.19 | -11.710 | -19.910 | -23.310 | -19.360 | -16.970 | -13.140 | -11.700 | -9.679  | -6.434 | -2.962 |
|       | 12.84 | -14.370 | -19.910 | -23.810 | -20.280 | -17.150 | -13.860 | -11.880 | -9.253  | -6.669 | -2.767 |
|       | 12.60 | -10.910 | -18.560 | -19.880 | -16.490 | -13.770 | -10.750 | -9.350  | -8.128  | -5.487 | -2.474 |
|       | 12.44 | -8.084  | -18.850 | -21.420 | -19.140 | -16.270 | -12.850 | -11.250 | -10.350 | -8.203 | -6.218 |
| ln(y) | 12.29 | -7.404  | -12.620 | -16.380 | -13.920 | -11.430 | -9.230  | -7.704  | -6.879  | -3.482 | -2.470 |
|       | 12.16 | -8.688  | -10.860 | -15.410 | -12.980 | -13.160 | -10.470 | -7.624  | -7.303  | -3.855 | -4.631 |
|       | 12.00 | -2.514  | -1.838  | -6.180  | -4.091  | -3.932  | -1.623  | 0.121   | 0.759   | 3.323  | 3.931  |
|       | 11.82 | 2.599   | -4.797  | -7.915  | -5.111  | -4.986  | -2.642  | -2.223  | -2.203  | -0.408 | 1.078  |
|       | 11.48 | 2.599   | -3.306  | -7.448  | -5.599  | -5.599  | -4.036  | -3.769  | -3.194  | -2.259 | -0.840 |
|       | 0.000 | -4.01   | -3.33   | -2.84   | -2.39   | -1.98   | -1.63   | -1.21   | -0.71   | 0.12   | 4.85   |
|       |       | HAZ     |         |         |         |         |         |         |         |        |        |

**Table A. 9 -  $\Pi^{1,1}$  Dominance Tests for Rural Toliara vs. Urban Areas in Madagascar**

| Urban Antananarivo           |       |        |        |        |        |        |        |        |        |        |        |
|------------------------------|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|                              | 16.51 | -0.085 | -0.023 | 0.778  | 1.441  | 2.923  | 0.675  | 1.065  | -0.932 | -0.712 | -0.239 |
|                              | 13.19 | -0.142 | 0.146  | 1.711  | 2.955  | 5.791  | 3.978  | 5.443  | 4.882  | 6.658  | 8.242  |
|                              | 12.84 | 0.858  | 3.064  | 3.881  | 6.683  | 9.403  | 8.289  | 10.760 | 10.850 | 12.560 | 14.140 |
|                              | 12.60 | 1.293  | 2.517  | 2.856  | 6.296  | 8.768  | 8.761  | 11.640 | 12.240 | 14.710 | 16.290 |
|                              | 12.44 | 2.711  | 4.168  | 4.808  | 8.222  | 10.750 | 12.460 | 15.980 | 16.890 | 20.300 | 21.750 |
| ln(y)                        | 12.29 | 2.668  | 4.449  | 5.027  | 8.769  | 11.520 | 12.600 | 15.170 | 15.470 | 18.910 | 20.120 |
|                              | 12.16 | 2.665  | 3.936  | 5.464  | 8.819  | 10.790 | 11.820 | 15.560 | 15.770 | 19.300 | 21.190 |
|                              | 12.00 | 2.270  | 2.904  | 5.020  | 8.523  | 11.300 | 11.640 | 14.820 | 16.500 | 20.330 | 22.990 |
|                              | 11.82 | 0.529  | 2.623  | 3.101  | 6.952  | 9.312  | 9.167  | 11.610 | 13.350 | 17.530 | 18.980 |
|                              | 11.48 | 0.159  | 0.789  | 2.245  | 7.929  | 9.939  | 10.520 | 12.340 | 13.860 | 16.160 | 17.270 |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|                              |       | HAZ    |        |        |        |        |        |        |        |        |        |
| Urban Fianarantsoa/Toamasina |       |        |        |        |        |        |        |        |        |        |        |
|                              | 16.51 | -1.133 | -3.948 | -0.593 | -1.625 | -1.623 | -0.509 | 2.390  | 1.748  | 1.224  | -0.239 |
|                              | 13.19 | -3.524 | -5.461 | -1.378 | -1.603 | -1.492 | 0.076  | 3.667  | 4.691  | 5.305  | 4.525  |
|                              | 12.84 | -3.135 | -5.698 | -1.722 | -1.087 | -0.353 | 1.784  | 5.640  | 7.322  | 8.479  | 7.570  |
|                              | 12.60 | -2.242 | -4.435 | -0.531 | 0.697  | 2.002  | 4.584  | 9.153  | 11.500 | 13.530 | 12.630 |
|                              | 12.44 | -1.596 | -3.442 | 0.813  | 2.032  | 4.605  | 7.247  | 11.850 | 14.680 | 16.480 | 15.270 |
| ln(y)                        | 12.29 | 0.100  | -3.008 | 0.858  | 2.011  | 4.975  | 7.091  | 11.160 | 13.560 | 15.220 | 13.950 |
|                              | 12.16 | 0.636  | -1.574 | 2.994  | 4.691  | 7.675  | 10.280 | 15.120 | 19.190 | 21.300 | 20.040 |
|                              | 12.00 | -0.099 | 0.672  | 4.114  | 7.895  | 11.330 | 13.470 | 17.850 | 22.080 | 24.370 | 24.130 |
|                              | 11.82 | -0.130 | 4.618  | 4.668  | 7.192  | 10.610 | 11.680 | 14.940 | 18.730 | 20.800 | 18.970 |
|                              | 11.48 | 0.392  | 3.094  | 5.193  | 9.621  | 12.310 | 13.170 | 16.630 | 18.330 | 20.920 | 22.040 |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|                              |       | HAZ    |        |        |        |        |        |        |        |        |        |
| Urban Mahajanga/Antsiranana  |       |        |        |        |        |        |        |        |        |        |        |
|                              | 16.51 | 11.240 | 8.615  | 10.680 | 8.802  | 6.980  | 3.459  | 1.641  | 2.241  | 0.723  | -0.239 |
|                              | 13.19 | 9.971  | 7.762  | 10.910 | 9.650  | 8.770  | 6.728  | 6.544  | 8.625  | 7.461  | 7.748  |
|                              | 12.84 | 9.453  | 7.292  | 9.933  | 10.880 | 10.770 | 8.449  | 9.714  | 12.130 | 10.350 | 11.220 |
|                              | 12.60 | 8.423  | 5.568  | 9.203  | 12.790 | 16.740 | 14.930 | 15.080 | 17.470 | 16.340 | 18.190 |
|                              | 12.44 | 8.423  | 9.161  | 12.090 | 16.950 | 21.570 | 19.250 | 21.450 | 24.190 | 24.960 | 27.430 |
| ln(y)                        | 12.29 | 7.375  | 7.780  | 10.930 | 16.510 | 21.310 | 19.120 | 20.550 | 23.530 | 24.890 | 27.720 |
|                              | 12.16 | 8.204  | 7.762  | 10.010 | 14.850 | 18.950 | 19.720 | 22.800 | 25.810 | 29.750 | 33.120 |
|                              | 12.00 | 6.437  | 7.891  | 9.729  | 14.530 | 18.240 | 18.890 | 21.970 | 25.060 | 29.290 | 32.190 |
|                              | 11.82 | 4.885  | 8.049  | 7.693  | 11.640 | 15.020 | 14.870 | 17.210 | 20.180 | 23.720 | 24.790 |
|                              | 11.48 | 2.191  | 4.735  | 3.574  | 8.400  | 10.980 | 11.220 | 14.720 | 15.560 | 17.470 | 18.590 |
|                              | 0.000 | -4.01  | -3.33  | -2.84  | -2.39  | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|                              |       | HAZ    |        |        |        |        |        |        |        |        |        |

Urban Toliara

|       |       |        |         |         |         |        |        |        |        |        |        |
|-------|-------|--------|---------|---------|---------|--------|--------|--------|--------|--------|--------|
|       | 16.51 | -8.841 | -16.320 | -16.580 | -11.430 | -8.068 | -6.658 | -4.174 | -2.208 | 0.022  | -0.239 |
|       | 13.19 | -9.286 | -16.780 | -16.090 | -11.080 | -7.815 | -6.221 | -3.662 | -0.933 | 2.005  | 2.118  |
|       | 12.84 | -9.845 | -15.690 | -15.930 | -10.720 | -7.053 | -5.253 | -2.017 | 1.018  | 3.969  | 4.288  |
|       | 12.60 | -3.307 | -11.960 | -9.174  | -3.734  | -0.638 | 1.677  | 5.642  | 8.312  | 11.250 | 11.090 |
|       | 12.44 | 1.646  | -10.230 | -7.667  | -2.467  | 0.711  | 3.174  | 7.454  | 10.100 | 13.360 | 13.260 |
| ln(y) | 12.29 | 1.263  | -6.159  | -3.925  | 1.479   | 5.464  | 7.136  | 10.410 | 12.260 | 16.550 | 15.620 |
|       | 12.16 | 0.628  | -3.287  | -2.195  | 2.421   | 5.733  | 7.625  | 12.410 | 14.220 | 18.720 | 17.440 |
|       | 12.00 | 6.766  | 4.360   | 6.195   | 10.920  | 14.140 | 15.600 | 19.430 | 21.820 | 26.530 | 27.180 |
|       | 11.82 | 7.153  | 4.561   | 4.882   | 8.766   | 12.440 | 13.510 | 15.620 | 17.350 | 22.040 | 22.570 |
|       | 11.48 | 5.048  | 1.268   | 1.683   | 7.348   | 10.780 | 11.660 | 13.610 | 14.920 | 16.750 | 17.340 |
|       | 0.000 | -4.01  | -3.33   | -2.84   | -2.39   | -1.98  | -1.63  | -1.21  | -0.71  | 0.12   | 4.85   |
|       |       | HAZ    |         |         |         |        |        |        |        |        |        |

**Table A. 10 -  $\Pi^{1,1}$  Dominance Tests for Rural and Urban Areas in Uganda**

|       |        |        |        |        |        |        |        |        |        |        |        |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|       | 11.660 | 13.600 | 16.660 | 14.920 | 15.060 | 12.410 | 8.983  | 8.863  | 7.301  | 2.382  | 0.023  |
|       | 9.276  | 14.340 | 20.740 | 22.210 | 25.370 | 23.980 | 23.510 | 24.900 | 25.220 | 24.210 | 25.460 |
|       | 8.996  | 14.950 | 21.230 | 22.860 | 28.670 | 26.790 | 27.070 | 31.150 | 32.820 | 32.090 | 34.140 |
|       | 8.803  | 16.610 | 23.260 | 25.680 | 30.690 | 32.420 | 33.130 | 37.380 | 39.530 | 40.910 | 42.910 |
|       | 8.664  | 15.440 | 21.360 | 23.380 | 27.810 | 30.120 | 31.610 | 34.830 | 38.300 | 40.620 | 43.490 |
| ln(y) | 8.527  | 14.340 | 20.720 | 22.390 | 27.500 | 30.650 | 32.860 | 35.580 | 38.370 | 40.340 | 43.050 |
|       | 8.395  | 13.390 | 21.030 | 22.510 | 26.720 | 30.920 | 33.620 | 35.930 | 38.280 | 39.870 | 42.230 |
|       | 8.249  | 12.180 | 18.820 | 19.990 | 23.150 | 26.520 | 28.810 | 31.280 | 33.140 | 34.490 | 36.030 |
|       | 8.068  | 9.106  | 15.410 | 16.730 | 19.730 | 22.550 | 25.010 | 27.170 | 29.930 | 31.040 | 33.400 |
|       | 7.824  | 7.643  | 12.440 | 14.980 | 17.960 | 19.510 | 21.790 | 23.680 | 25.490 | 25.990 | 27.460 |
|       | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|       |        |        |        |        |        |        |        |        |        |        | HAZ    |

**Table A. 11 -  $\Pi^{1,1}$  Dominance Tests for Rural Central vs. Urban Areas in Uganda**

| Urban Central |        |        |        |        |        |        |        |        |        |        |        |
|---------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 11.660 | 12.760 | 13.100 | 12.840 | 13.710 | 9.432  | 5.963  | 5.357  | 4.718  | 0.572  | 0.023  |
|               | 9.276  | 12.960 | 17.960 | 22.720 | 26.110 | 23.090 | 22.510 | 22.680 | 24.320 | 24.900 | 27.770 |
|               | 8.996  | 12.500 | 17.740 | 22.160 | 28.870 | 24.500 | 23.900 | 28.360 | 31.210 | 31.820 | 34.560 |
|               | 8.803  | 15.220 | 20.370 | 26.060 | 31.410 | 32.120 | 31.720 | 35.410 | 37.910 | 41.590 | 43.530 |
|               | 8.664  | 11.640 | 15.770 | 20.210 | 25.220 | 25.990 | 26.390 | 28.990 | 32.390 | 36.670 | 39.410 |
| ln(y)         | 8.527  | 9.674  | 14.220 | 18.040 | 23.550 | 25.530 | 26.110 | 27.800 | 29.710 | 33.160 | 34.950 |
|               | 8.395  | 7.385  | 14.410 | 16.980 | 21.230 | 24.020 | 25.000 | 25.790 | 27.030 | 29.260 | 30.280 |
|               | 8.249  | 6.545  | 11.620 | 14.430 | 16.940 | 18.860 | 18.860 | 20.690 | 20.540 | 21.920 | 21.750 |
|               | 8.068  | 3.557  | 9.455  | 12.730 | 15.580 | 16.630 | 17.640 | 19.740 | 21.380 | 21.440 | 22.700 |
|               | 7.824  | 4.698  | 7.724  | 9.413  | 10.800 | 12.110 | 14.010 | 15.930 | 16.730 | 16.090 | 16.900 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | HAZ    |
| Urban Eastern |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 2.637  | 12.510 | 8.720  | 7.938  | 9.993  | 7.941  | 11.170 | 4.484  | 1.109  | 0.000  |
|               | 9.276  | 3.458  | 13.930 | 9.712  | 12.030 | 15.540 | 15.410 | 20.020 | 13.550 | 14.130 | 16.400 |
|               | 8.996  | 5.519  | 14.940 | 10.590 | 13.920 | 17.110 | 17.110 | 22.360 | 18.330 | 18.410 | 20.250 |
|               | 8.803  | 2.559  | 11.910 | 7.156  | 10.320 | 13.760 | 14.730 | 21.160 | 18.730 | 19.030 | 21.460 |
|               | 8.664  | 0.610  | 8.643  | 4.224  | 7.651  | 9.988  | 9.820  | 15.270 | 15.010 | 16.430 | 19.950 |
| ln(y)         | 8.527  | 0.062  | 8.763  | 5.016  | 8.366  | 9.201  | 12.340 | 17.300 | 15.860 | 17.390 | 19.570 |
|               | 8.395  | -2.842 | 5.754  | -0.025 | 2.692  | 4.249  | 6.958  | 10.650 | 12.260 | 13.580 | 15.240 |
|               | 8.249  | -1.582 | 5.582  | -0.307 | 2.743  | 2.801  | 5.305  | 8.590  | 11.310 | 13.020 | 13.520 |
|               | 8.068  | -4.756 | 1.731  | -4.960 | -1.046 | 0.140  | 2.003  | 4.765  | 6.872  | 9.221  | 8.636  |
|               | 7.824  | 4.698  | 8.001  | 8.184  | 9.695  | 7.846  | 10.090 | 12.120 | 12.850 | 13.900 | 12.290 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | HAZ    |
| Urban Western |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 7.881  | 10.700 | 17.210 | 15.520 | 14.030 | 10.990 | 11.270 | 10.440 | 5.947  | 0.167  |
|               | 9.276  | 8.307  | 15.070 | 24.580 | 28.270 | 25.850 | 24.640 | 28.660 | 34.110 | 30.540 | 30.250 |
|               | 8.996  | 8.272  | 14.840 | 23.080 | 27.160 | 25.870 | 27.190 | 30.100 | 36.320 | 34.660 | 39.630 |
|               | 8.803  | 8.478  | 15.800 | 22.990 | 27.460 | 28.090 | 30.370 | 34.940 | 41.120 | 41.830 | 46.850 |
| ln(y)         | 8.664  | 6.314  | 16.500 | 23.720 | 27.180 | 28.020 | 30.250 | 33.390 | 38.370 | 41.150 | 46.240 |
|               | 8.527  | 6.429  | 15.730 | 22.070 | 26.120 | 25.370 | 26.910 | 29.410 | 32.860 | 34.600 | 37.110 |
|               | 8.395  | 4.164  | 11.510 | 17.150 | 23.180 | 23.800 | 25.810 | 27.870 | 31.160 | 32.300 | 34.120 |
|               | 8.249  | 4.245  | 8.491  | 13.760 | 19.610 | 21.630 | 22.310 | 23.440 | 25.160 | 26.790 | 27.890 |
|               | 8.068  | 7.488  | 12.370 | 15.210 | 18.610 | 20.080 | 20.920 | 22.760 | 24.650 | 26.820 | 28.010 |
|               | 7.824  | 4.698  | 8.001  | 9.646  | 11.000 | 12.980 | 14.790 | 16.640 | 17.410 | 18.540 | 19.270 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | HAZ    |

Urban Northern

|       |        |         |        |         |         |         |        |        |        |        |        |
|-------|--------|---------|--------|---------|---------|---------|--------|--------|--------|--------|--------|
|       | 11.660 | -2.078  | 8.260  | 1.118   | 0.875   | -8.225  | -6.702 | -5.046 | -4.178 | -1.944 | 0.000  |
|       | 9.276  | -3.019  | 6.890  | -0.340  | 0.249   | -8.063  | -6.814 | -4.963 | -3.129 | 0.715  | 3.785  |
|       | 8.996  | -4.014  | 4.852  | -3.787  | -2.839  | -10.300 | -9.337 | -8.146 | -4.784 | -1.764 | 0.788  |
|       | 8.803  | -3.698  | 4.300  | -3.206  | -2.787  | -6.477  | -6.524 | -5.319 | -2.051 | 0.400  | 2.425  |
|       | 8.664  | -5.033  | 1.988  | -6.463  | -6.171  | -8.087  | -8.878 | -8.893 | -6.401 | -3.475 | -0.626 |
| ln(y) | 8.527  | -7.906  | 0.136  | -9.609  | -6.720  | -6.885  | -7.752 | -6.152 | -4.600 | -0.948 | 0.039  |
|       | 8.395  | -1.872  | 1.605  | -3.988  | -1.914  | 1.728   | 3.549  | 3.473  | 4.507  | 7.883  | 9.095  |
|       | 8.249  | -5.686  | -4.736 | -10.610 | -9.483  | -6.670  | -3.696 | -1.952 | -2.388 | 0.348  | 1.345  |
|       | 8.068  | -8.670  | -6.032 | -8.345  | -10.410 | -7.781  | -5.557 | -4.831 | -4.195 | -1.707 | -1.636 |
|       | 7.824  | -10.520 | -6.723 | -4.552  | -2.706  | -0.172  | 2.293  | 4.761  | 5.295  | 6.767  | 7.456  |
|       | 0.000  | -3.100  | -2.450 | -1.970  | -1.580  | -1.220  | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|       |        |         |        |         |         |         |        |        |        |        | HAZ    |

**Table A. 12 -  $\Pi^{1,1}$  Dominance Tests for Rural Eastern vs. Urban Areas in Uganda**

| Urban Central |        |        |        |        |        |        |        |        |        |        |        |
|---------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 11.660 | 17.010 | 15.740 | 13.760 | 14.930 | 12.370 | 8.695  | 8.636  | 8.251  | 2.570  | -0.009 |
|               | 9.276  | 18.070 | 21.710 | 25.220 | 29.350 | 28.460 | 28.470 | 29.620 | 31.460 | 30.110 | 31.160 |
|               | 8.996  | 18.270 | 22.340 | 26.690 | 35.020 | 32.870 | 33.410 | 39.490 | 42.530 | 41.420 | 42.790 |
|               | 8.803  | 21.890 | 26.520 | 33.030 | 40.110 | 43.030 | 43.890 | 49.210 | 52.650 | 55.750 | 56.790 |
|               | 8.664  | 20.380 | 24.090 | 29.390 | 35.670 | 39.260 | 42.040 | 46.420 | 51.940 | 55.810 | 58.080 |
| ln(y)         | 8.527  | 18.530 | 22.750 | 27.360 | 33.830 | 39.060 | 41.610 | 44.990 | 49.520 | 52.240 | 54.790 |
|               | 8.395  | 16.170 | 23.810 | 27.760 | 32.930 | 38.360 | 40.970 | 44.020 | 46.850 | 48.860 | 50.780 |
|               | 8.249  | 15.140 | 21.560 | 25.040 | 27.970 | 32.200 | 33.720 | 36.860 | 38.500 | 39.930 | 40.690 |
|               | 8.068  | 12.850 | 18.470 | 21.890 | 24.590 | 27.680 | 29.710 | 32.190 | 35.350 | 36.220 | 38.270 |
|               | 7.824  | 10.100 | 13.140 | 14.760 | 16.910 | 18.870 | 21.010 | 22.700 | 25.040 | 25.410 | 26.570 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | HAZ    |
| Urban Eastern |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 7.033  | 15.150 | 9.633  | 9.146  | 12.930 | 10.690 | 14.510 | 8.015  | 3.108  | -0.032 |
|               | 9.276  | 8.785  | 17.670 | 12.130 | 15.080 | 20.690 | 21.110 | 26.830 | 20.180 | 18.970 | 19.520 |
|               | 8.996  | 11.550 | 19.560 | 15.020 | 19.690 | 25.140 | 26.220 | 32.960 | 28.470 | 26.940 | 27.450 |
|               | 8.803  | 10.050 | 18.190 | 13.980 | 18.400 | 23.630 | 25.610 | 33.380 | 31.090 | 30.350 | 31.950 |
|               | 8.664  | 10.360 | 17.170 | 13.400 | 17.690 | 22.450 | 24.180 | 31.130 | 32.010 | 32.370 | 35.290 |
| ln(y)         | 8.527  | 10.000 | 17.580 | 14.540 | 18.550 | 22.220 | 27.030 | 33.520 | 33.920 | 34.270 | 36.930 |
|               | 8.395  | 7.007  | 16.030 | 11.570 | 14.780 | 18.630 | 22.510 | 28.060 | 30.850 | 31.590 | 33.880 |
|               | 8.249  | 8.414  | 16.640 | 11.640 | 14.580 | 16.850 | 20.480 | 24.780 | 29.100 | 30.690 | 32.000 |
|               | 8.068  | 5.731  | 12.210 | 6.121  | 9.568  | 12.730 | 15.290 | 18.210 | 21.720 | 24.540 | 24.690 |
|               | 7.824  | 10.100 | 13.310 | 13.910 | 16.150 | 15.590 | 17.940 | 19.620 | 21.990 | 23.640 | 22.780 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | HAZ    |
| Urban Western |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 12.230 | 13.330 | 18.140 | 16.760 | 17.010 | 13.760 | 14.610 | 14.040 | 7.962  | 0.135  |
|               | 9.276  | 13.560 | 18.810 | 27.100 | 31.560 | 31.320 | 30.690 | 35.950 | 41.940 | 36.030 | 33.720 |
|               | 8.996  | 14.230 | 19.460 | 27.620 | 33.260 | 34.320 | 36.940 | 41.410 | 48.280 | 44.560 | 48.360 |
|               | 8.803  | 15.730 | 22.040 | 29.950 | 36.030 | 38.730 | 42.420 | 48.680 | 56.400 | 56.030 | 60.700 |
| ln(y)         | 8.664  | 15.720 | 24.780 | 32.840 | 37.660 | 41.410 | 46.280 | 51.470 | 59.130 | 61.300 | 66.580 |
|               | 8.527  | 15.810 | 24.150 | 31.210 | 36.380 | 38.900 | 42.460 | 46.770 | 53.160 | 53.930 | 57.390 |
|               | 8.395  | 13.500 | 21.300 | 27.910 | 34.770 | 38.150 | 41.780 | 46.200 | 51.360 | 52.280 | 55.200 |
|               | 8.249  | 13.440 | 19.100 | 24.480 | 30.330 | 34.680 | 36.960 | 39.530 | 43.120 | 44.940 | 47.150 |
|               | 8.068  | 15.200 | 20.460 | 23.690 | 26.950 | 30.420 | 32.440 | 34.810 | 38.210 | 41.060 | 43.100 |
|               | 7.824  | 10.100 | 13.310 | 14.920 | 17.050 | 19.490 | 21.580 | 23.240 | 25.550 | 27.290 | 28.410 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | HAZ    |

Urban Northern

|       |        |        |        |        |        |        |        |        |        |        |        |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|       | 11.660 | 2.327  | 10.890 | 2.023  | 2.072  | -5.318 | -3.980 | -1.786 | -0.666 | 0.054  | -0.032 |
|       | 9.276  | 2.331  | 10.620 | 2.051  | 3.234  | -3.114 | -1.367 | 1.307  | 3.208  | 5.342  | 6.751  |
|       | 8.996  | 2.091  | 9.473  | 0.586  | 2.751  | -2.662 | -0.767 | 1.374  | 4.544  | 6.115  | 7.378  |
|       | 8.803  | 3.852  | 10.610 | 3.570  | 5.122  | 3.006  | 3.806  | 5.738  | 9.270  | 10.780 | 11.910 |
|       | 8.664  | 4.792  | 10.580 | 2.684  | 3.735  | 4.042  | 5.005  | 5.930  | 9.383  | 11.210 | 13.200 |
| ln(y) | 8.527  | 2.090  | 9.130  | -0.079 | 3.370  | 5.877  | 6.406  | 8.982  | 12.200 | 14.660 | 15.820 |
|       | 8.395  | 7.952  | 12.070 | 7.623  | 10.160 | 16.080 | 19.020 | 20.570 | 22.620 | 25.470 | 27.200 |
|       | 8.249  | 4.379  | 6.944  | 1.347  | 2.396  | 7.387  | 11.440 | 14.100 | 15.070 | 17.570 | 19.270 |
|       | 8.068  | 1.615  | 4.746  | 2.698  | 0.182  | 4.861  | 7.806  | 8.691  | 10.730 | 13.640 | 14.390 |
|       | 7.824  | -3.933 | 0.459  | 2.634  | 5.474  | 8.455  | 11.080 | 13.110 | 15.430 | 17.470 | 18.520 |
|       | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|       |        |        |        |        |        |        |        |        |        |        | HAZ    |

**Table A. 13 -  $\Pi^{1,1}$  Dominance Tests for Rural Western vs. Urban Areas in Uganda**

| Urban Central |        |        |        |        |        |        |        |        |        |        |        |
|---------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 11.660 | 20.570 | 21.990 | 22.390 | 23.130 | 19.630 | 13.880 | 11.400 | 9.372  | 3.245  | 0.023  |
|               | 9.276  | 20.580 | 26.270 | 31.970 | 35.810 | 33.640 | 31.330 | 29.580 | 29.480 | 28.090 | 27.970 |
|               | 8.996  | 20.590 | 25.980 | 31.940 | 39.620 | 35.750 | 33.910 | 37.060 | 37.870 | 36.670 | 37.010 |
|               | 8.803  | 23.020 | 28.260 | 35.700 | 41.600 | 43.280 | 41.360 | 43.770 | 44.580 | 46.270 | 45.680 |
|               | 8.664  | 20.960 | 24.890 | 31.180 | 35.380 | 37.500 | 37.520 | 38.590 | 40.680 | 42.990 | 43.550 |
| ln(y)         | 8.527  | 18.830 | 23.370 | 28.750 | 33.420 | 37.260 | 37.410 | 37.290 | 38.970 | 40.790 | 41.980 |
|               | 8.395  | 16.520 | 24.000 | 28.470 | 31.660 | 35.930 | 36.560 | 36.200 | 36.300 | 37.430 | 38.000 |
|               | 8.249  | 14.220 | 21.170 | 25.200 | 26.300 | 28.870 | 29.220 | 29.580 | 29.310 | 29.290 | 29.000 |
|               | 8.068  | 10.220 | 16.640 | 19.930 | 21.810 | 22.990 | 24.370 | 25.150 | 26.410 | 25.390 | 27.410 |
|               | 7.824  | 7.087  | 10.400 | 12.300 | 14.070 | 14.310 | 15.350 | 16.110 | 16.590 | 15.380 | 16.180 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | haz    |
| Urban Eastern |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 10.720 | 21.400 | 18.150 | 17.150 | 20.220 | 15.920 | 17.340 | 9.136  | 3.783  | 0.000  |
|               | 9.276  | 11.400 | 22.210 | 18.550 | 21.030 | 25.610 | 23.820 | 26.790 | 18.360 | 17.100 | 16.590 |
|               | 8.996  | 13.960 | 23.200 | 20.070 | 23.890 | 27.870 | 26.690 | 30.660 | 24.350 | 22.760 | 22.420 |
|               | 8.803  | 11.300 | 19.950 | 16.530 | 19.730 | 23.850 | 23.400 | 28.650 | 24.460 | 22.890 | 23.230 |
|               | 8.664  | 11.000 | 17.990 | 15.160 | 17.420 | 20.840 | 20.140 | 24.150 | 22.440 | 21.910 | 23.500 |
| ln(y)         | 8.527  | 10.340 | 18.220 | 15.940 | 18.150 | 20.530 | 23.140 | 26.360 | 24.490 | 24.320 | 25.910 |
|               | 8.395  | 7.405  | 16.240 | 12.320 | 13.490 | 16.270 | 18.340 | 20.760 | 21.150 | 21.280 | 22.460 |
|               | 8.249  | 7.343  | 16.210 | 11.820 | 12.810 | 13.400 | 15.950 | 17.600 | 20.090 | 20.340 | 20.700 |
|               | 8.068  | 2.642  | 10.110 | 3.759  | 6.335  | 7.454  | 9.488  | 10.690 | 12.320 | 13.390 | 13.600 |
|               | 7.824  | 7.087  | 10.610 | 11.310 | 13.190 | 10.430 | 11.630 | 12.320 | 12.690 | 13.130 | 11.490 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | haz    |
| Urban Western |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 15.870 | 19.560 | 26.930 | 25.030 | 24.460 | 19.060 | 17.450 | 15.190 | 8.643  | 0.167  |
|               | 9.276  | 16.130 | 23.360 | 33.900 | 38.120 | 36.620 | 33.600 | 35.910 | 39.750 | 33.890 | 30.450 |
|               | 8.996  | 16.610 | 23.100 | 32.890 | 37.800 | 37.230 | 37.450 | 38.930 | 43.330 | 39.650 | 42.210 |
|               | 8.803  | 16.940 | 23.790 | 32.600 | 37.480 | 38.970 | 39.920 | 43.270 | 48.000 | 46.520 | 49.080 |
| ln(y)         | 8.664  | 16.330 | 25.580 | 34.630 | 37.370 | 39.640 | 41.620 | 43.300 | 47.070 | 47.740 | 50.680 |
|               | 8.527  | 16.130 | 24.760 | 32.590 | 35.960 | 37.100 | 38.240 | 38.980 | 42.300 | 42.300 | 44.270 |
|               | 8.395  | 13.870 | 21.500 | 28.630 | 33.500 | 35.720 | 37.360 | 38.310 | 40.530 | 40.580 | 41.990 |
|               | 8.249  | 12.470 | 18.680 | 24.650 | 28.690 | 31.400 | 32.480 | 32.250 | 33.860 | 34.150 | 35.180 |
|               | 8.068  | 12.890 | 18.760 | 21.830 | 24.330 | 25.960 | 27.290 | 27.950 | 29.470 | 30.550 | 32.480 |
|               | 7.824  | 7.087  | 10.610 | 12.490 | 14.240 | 15.080 | 16.080 | 16.810 | 17.270 | 17.880 | 18.620 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | haz    |

Urban Northern

|       |        |        |        |        |        |        |        |        |        |        |        |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|       | 11.660 | 6.026  | 17.090 | 10.400 | 9.926  | 1.684  | 1.108  | 0.937  | 0.440  | 0.728  | 0.000  |
|       | 9.276  | 4.961  | 15.120 | 8.337  | 8.974  | 1.449  | 1.148  | 1.273  | 1.487  | 3.568  | 3.963  |
|       | 8.996  | 4.551  | 13.090 | 5.502  | 6.744  | -0.173 | -0.338 | -0.614 | 0.838  | 2.310  | 2.808  |
|       | 8.803  | 5.125  | 12.370 | 6.080  | 6.413  | 3.208  | 1.760  | 1.586  | 3.306  | 4.016  | 4.061  |
|       | 8.664  | 5.443  | 11.400 | 4.421  | 3.468  | 2.518  | 1.198  | -0.397 | 0.700  | 1.727  | 2.698  |
| ln(y) | 8.527  | 2.436  | 9.777  | 1.311  | 2.975  | 4.255  | 2.752  | 2.490  | 3.639  | 5.633  | 5.988  |
|       | 8.395  | 8.347  | 12.280 | 8.380  | 8.881  | 13.730 | 14.880 | 13.460 | 13.250 | 15.460 | 16.170 |
|       | 8.249  | 3.273  | 6.477  | 1.536  | 0.620  | 3.949  | 6.952  | 7.031  | 6.331  | 7.580  | 8.409  |
|       | 8.068  | -1.524 | 2.535  | 0.324  | -3.083 | -0.469 | 1.955  | 1.128  | 1.292  | 2.492  | 3.349  |
|       | 7.824  | -7.871 | -3.246 | -0.675 | 1.715  | 2.677  | 4.016  | 4.981  | 5.118  | 5.921  | 6.609  |
|       | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|       |        |        |        |        |        |        |        |        |        |        | haz    |

**Table A. 14 -  $\Pi^{1,1}$  Dominance Tests for Rural Northern vs. Urban Areas in Uganda**

| Urban Central |        |        |        |        |        |        |        |        |        |        |        |
|---------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 11.660 | 19.720 | 18.840 | 16.170 | 16.690 | 11.790 | 7.597  | 6.035  | 6.904  | 0.391  | 0.023  |
|               | 9.276  | 21.280 | 25.590 | 28.750 | 32.190 | 28.870 | 28.590 | 28.300 | 31.410 | 29.330 | 33.140 |
|               | 8.996  | 21.780 | 27.460 | 31.300 | 39.420 | 35.430 | 36.110 | 40.820 | 45.510 | 44.060 | 49.000 |
|               | 8.803  | 26.170 | 33.100 | 39.110 | 46.940 | 48.670 | 50.600 | 55.650 | 61.370 | 64.140 | 69.890 |
|               | 8.664  | 24.370 | 30.680 | 36.570 | 44.500 | 47.280 | 51.100 | 55.400 | 63.730 | 68.000 | 74.460 |
| ln(y)         | 8.527  | 24.190 | 30.940 | 37.130 | 45.970 | 51.050 | 55.740 | 59.210 | 66.610 | 70.030 | 78.270 |
|               | 8.395  | 23.440 | 32.790 | 38.570 | 46.070 | 52.330 | 57.590 | 61.310 | 67.130 | 69.920 | 77.660 |
|               | 8.249  | 21.400 | 30.450 | 36.640 | 43.320 | 49.440 | 53.360 | 57.880 | 62.020 | 64.490 | 70.570 |
|               | 8.068  | 17.160 | 25.550 | 33.000 | 39.910 | 44.450 | 49.020 | 53.480 | 59.330 | 60.190 | 68.530 |
|               | 7.824  | 15.210 | 22.720 | 27.610 | 33.360 | 37.020 | 41.050 | 44.620 | 48.220 | 48.980 | 54.140 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | haz    |
| Urban Eastern |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 9.834  | 18.250 | 12.020 | 10.870 | 12.360 | 9.584  | 11.860 | 6.669  | 0.927  | 0.000  |
|               | 9.276  | 12.110 | 21.540 | 15.500 | 17.710 | 21.090 | 21.230 | 25.530 | 20.130 | 18.250 | 21.320 |
|               | 8.996  | 15.200 | 24.680 | 19.460 | 23.720 | 27.560 | 28.770 | 34.200 | 31.050 | 29.220 | 32.690 |
|               | 8.803  | 14.780 | 24.820 | 19.750 | 24.440 | 28.510 | 31.320 | 38.830 | 37.890 | 36.540 | 41.410 |
|               | 8.664  | 14.750 | 23.850 | 20.370 | 25.790 | 29.610 | 32.000 | 38.850 | 41.390 | 41.540 | 47.330 |
| ln(y)         | 8.527  | 16.280 | 25.940 | 24.240 | 30.020 | 33.080 | 39.630 | 46.240 | 48.250 | 48.590 | 55.310 |
|               | 8.395  | 15.170 | 25.550 | 22.690 | 27.510 | 31.530 | 37.350 | 43.260 | 48.170 | 49.060 | 55.640 |
|               | 8.249  | 15.570 | 26.120 | 24.090 | 30.180 | 33.730 | 39.190 | 44.440 | 51.040 | 53.370 | 59.320 |
|               | 8.068  | 10.750 | 20.090 | 18.880 | 26.310 | 30.350 | 34.890 | 39.250 | 44.840 | 47.440 | 52.680 |
|               | 7.824  | 15.210 | 22.830 | 27.070 | 32.880 | 34.720 | 38.810 | 42.300 | 45.800 | 47.500 | 50.830 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | haz    |
| Urban Western |        |        |        |        |        |        |        |        |        |        |        |
|               | 11.660 | 15.000 | 16.420 | 20.590 | 18.520 | 16.430 | 12.650 | 11.960 | 12.670 | 5.765  | 0.167  |
|               | 9.276  | 16.840 | 22.680 | 30.650 | 34.430 | 31.740 | 30.810 | 34.550 | 41.890 | 35.200 | 35.760 |
|               | 8.996  | 17.840 | 24.580 | 32.240 | 37.610 | 36.900 | 39.720 | 42.770 | 51.460 | 47.300 | 55.030 |
|               | 8.803  | 20.310 | 28.660 | 35.970 | 42.680 | 44.170 | 49.030 | 55.080 | 65.570 | 64.460 | 74.610 |
| ln(y)         | 8.664  | 19.940 | 31.360 | 40.060 | 46.590 | 49.570 | 55.720 | 60.980 | 72.090 | 74.470 | 85.300 |
|               | 8.527  | 21.720 | 32.270 | 40.950 | 48.620 | 50.880 | 56.700 | 61.260 | 71.050 | 72.130 | 81.810 |
|               | 8.395  | 21.110 | 30.490 | 38.720 | 47.920 | 52.110 | 58.490 | 63.830 | 72.660 | 74.220 | 83.800 |
|               | 8.249  | 19.980 | 28.310 | 36.140 | 45.550 | 51.920 | 56.800 | 60.870 | 67.510 | 70.650 | 79.260 |
|               | 8.068  | 19.130 | 27.190 | 34.450 | 41.860 | 46.860 | 51.580 | 56.050 | 62.310 | 65.420 | 74.170 |
|               | 7.824  | 15.210 | 22.830 | 27.700 | 33.450 | 37.430 | 41.450 | 45.020 | 48.610 | 50.510 | 55.680 |
|               | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|               |        |        |        |        |        |        |        |        |        |        | haz    |

Urban Northern

|       |        |        |        |        |        |        |        |        |        |        |        |
|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|       | 11.660 | 5.139  | 13.970 | 4.385  | 3.772  | -5.883 | -5.070 | -4.368 | -2.001 | -2.125 | 0.000  |
|       | 9.276  | 5.686  | 14.450 | 5.364  | 5.787  | -2.739 | -1.261 | 0.137  | 3.163  | 4.662  | 8.447  |
|       | 8.996  | 5.817  | 14.550 | 4.910  | 6.578  | -0.447 | 1.526  | 2.435  | 6.813  | 8.149  | 11.990 |
|       | 8.803  | 8.658  | 17.220 | 9.218  | 10.910 | 7.505  | 8.951  | 10.330 | 15.130 | 16.170 | 19.940 |
|       | 8.664  | 9.272  | 17.280 | 9.535  | 11.510 | 10.710 | 12.140 | 12.570 | 17.370 | 19.010 | 23.110 |
| ln(y) | 8.527  | 8.582  | 17.610 | 9.460  | 14.360 | 16.040 | 17.700 | 19.780 | 24.290 | 26.780 | 30.780 |
|       | 8.395  | 16.060 | 21.740 | 18.730 | 22.770 | 28.860 | 33.580 | 35.030 | 38.820 | 42.000 | 47.480 |
|       | 8.249  | 11.830 | 17.050 | 13.930 | 17.860 | 23.930 | 29.560 | 32.740 | 35.140 | 38.170 | 43.700 |
|       | 8.068  | 6.808  | 13.120 | 15.570 | 17.100 | 22.510 | 27.260 | 29.330 | 33.020 | 35.550 | 40.860 |
|       | 7.824  | 3.033  | 12.760 | 18.520 | 24.940 | 29.090 | 33.300 | 36.960 | 40.200 | 42.080 | 46.940 |
|       | 0.000  | -3.100 | -2.450 | -1.970 | -1.580 | -1.220 | -0.880 | -0.500 | -0.010 | 0.690  | 5.820  |
|       |        |        |        |        |        |        |        |        |        |        | haz    |